

Studying Nucleon Structure with Spin at BLAST

Overview
BLAST Experiment
Nucleon Form Factors
Deuterium

Nucleon Elastic Form Factors

Fundamental for understanding nucleon structure in non-perturbative regime.

Parameterises coherent scattering without exciting internal degrees of freedom with single photon exchange.

- for point-like, spin=1/2 particles QED gives:

$$\sigma_{Dirac} = \sigma_{Mott} \left(1 + 2\tau \tan^2 \frac{\theta}{2} \right)$$

- for extended objects, like nucleons, require form factors:

$$\sigma_{lab} = \sigma_{Mott} \left[\left(\frac{G_E^N{}^2 + \tau G_M^N{}^2}{1 + \tau} \right) + 2\tau G_M^N{}^2 \tan^2 \frac{\theta}{2} \right]$$

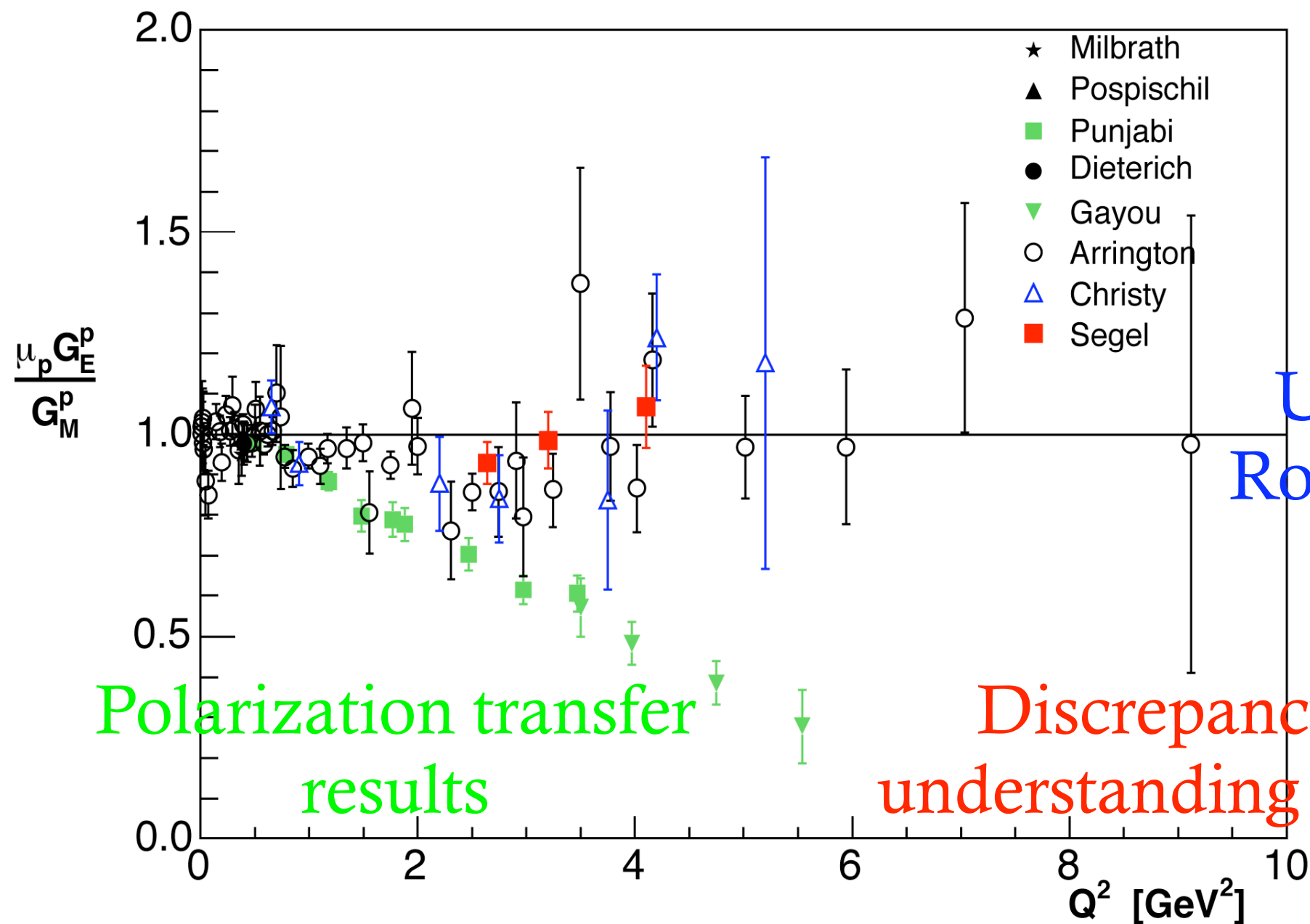
- traditionally measure using Rosenbluth technique

$$\sigma_{Rosenbluth} = \sigma_{Mott} \left(A^N(Q^2) + 2\tau B^N(Q^2) \tan^2 \frac{\theta}{2} \right)$$

Discrepancy in Proton Form Factor Ratio

Polarization transfer results
in striking discrepancy with
unpolarized data

Possible explanation
- two photon contributions



Unpolarised results
Rosenbluth separation

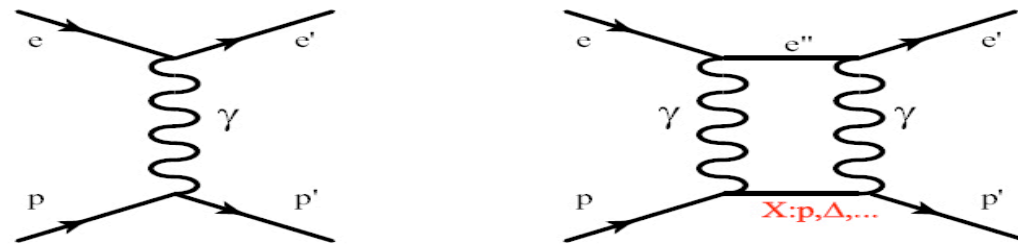
Polarization transfer
results

Discrepancy fundamental to
understanding of nucleon structure

Importance of Spin Measurements

JLAB results highlight the importance of using spin in studying nucleon structure

- more information
- more detailed information



A Definitive Experiment to Quantify Multi-photon Exchange in Lepton Scattering

M. Kohl, MIT

09:00 Thursday

Nucleon Elastic Form Factors

Parameterised as dipole distribution in momentum space.

- corresponds to a exponential distribution in position space
- single dipole describes G_E^p , G_M^p , and G_M^n
- G_E^n is the exception, order of magnitude smaller
 - traditionally hard to measure, small, no convenient neutron targets

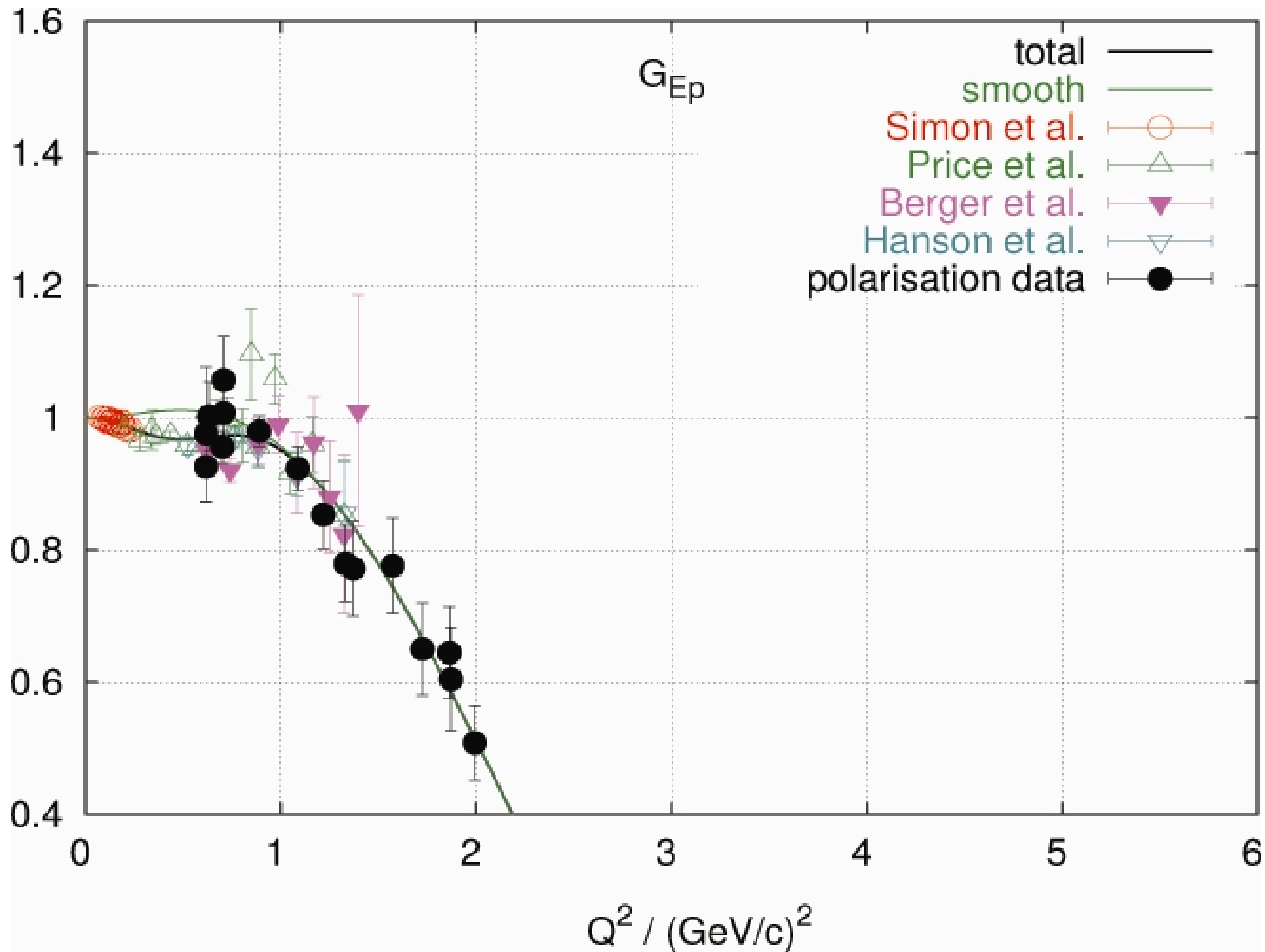
But dipole not perfect, does not describe details $Q^2 < 1 \text{ (GeV/c)}^2$

Friedrich and Walcher have proposed a new parameterisation:

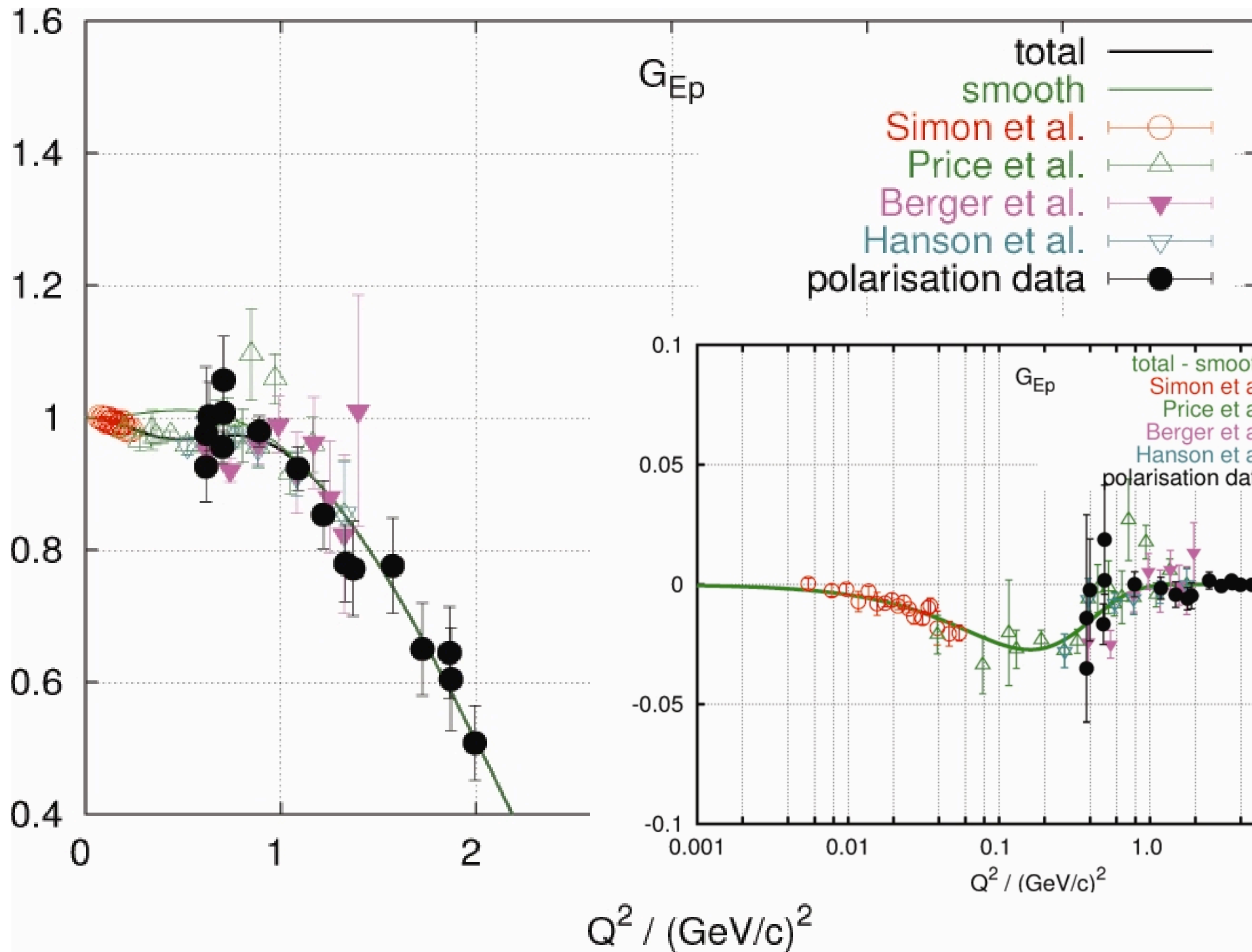
$$G^N(Q^2) = G_S^N(Q^2) + \alpha_B Q^2 G_B^N(Q^2)$$

- S- smooth term of two dipoles
- B - bump part of two gaussians
- fit to a collection of the world's data

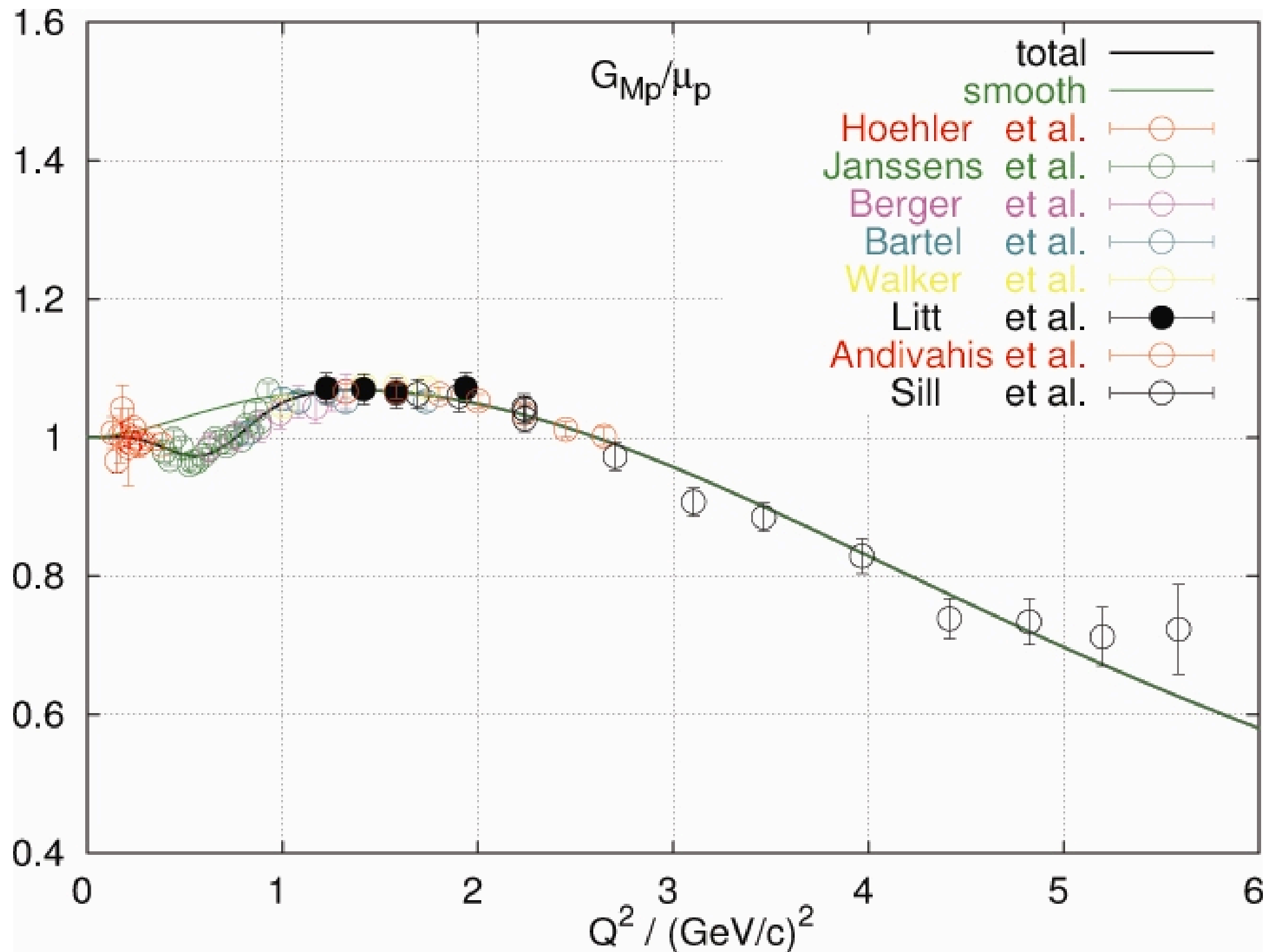
Friedrich and Walcher Fit to G_E^p



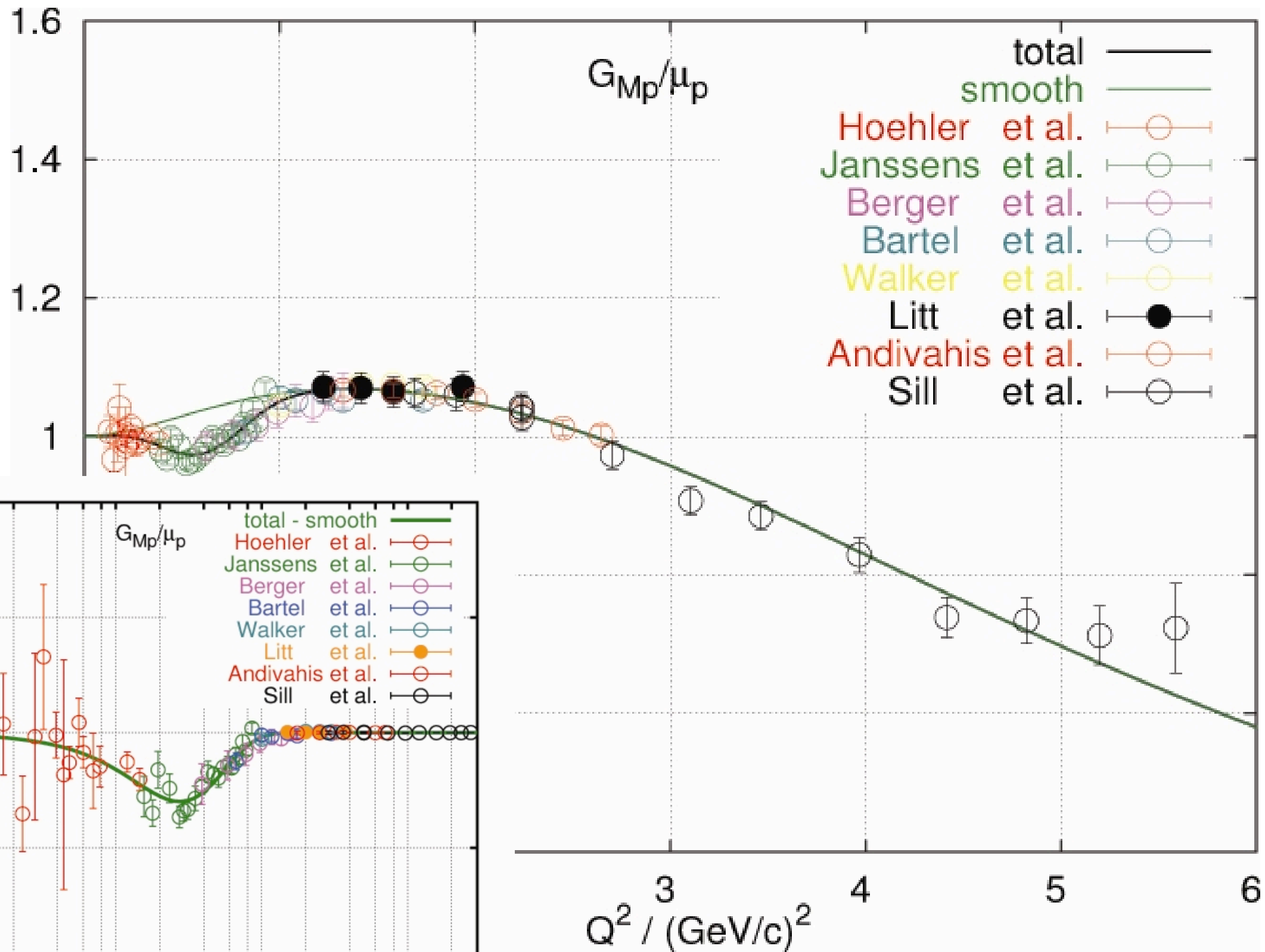
Friedrich and Walcher Fit to G_E^p



Friedrich and Walcher Fit to G_M^p



Friedrich and Walcher Fit to G_M^p



Bates Large Acceptance Spectrometer Toroid

Systematic study of spin-dependent electromagnetic interaction

Polarized electrons in MIT-Bates SHR storage ring

- 850 MeV, 200 mA (typical), 65% polarization (typical)

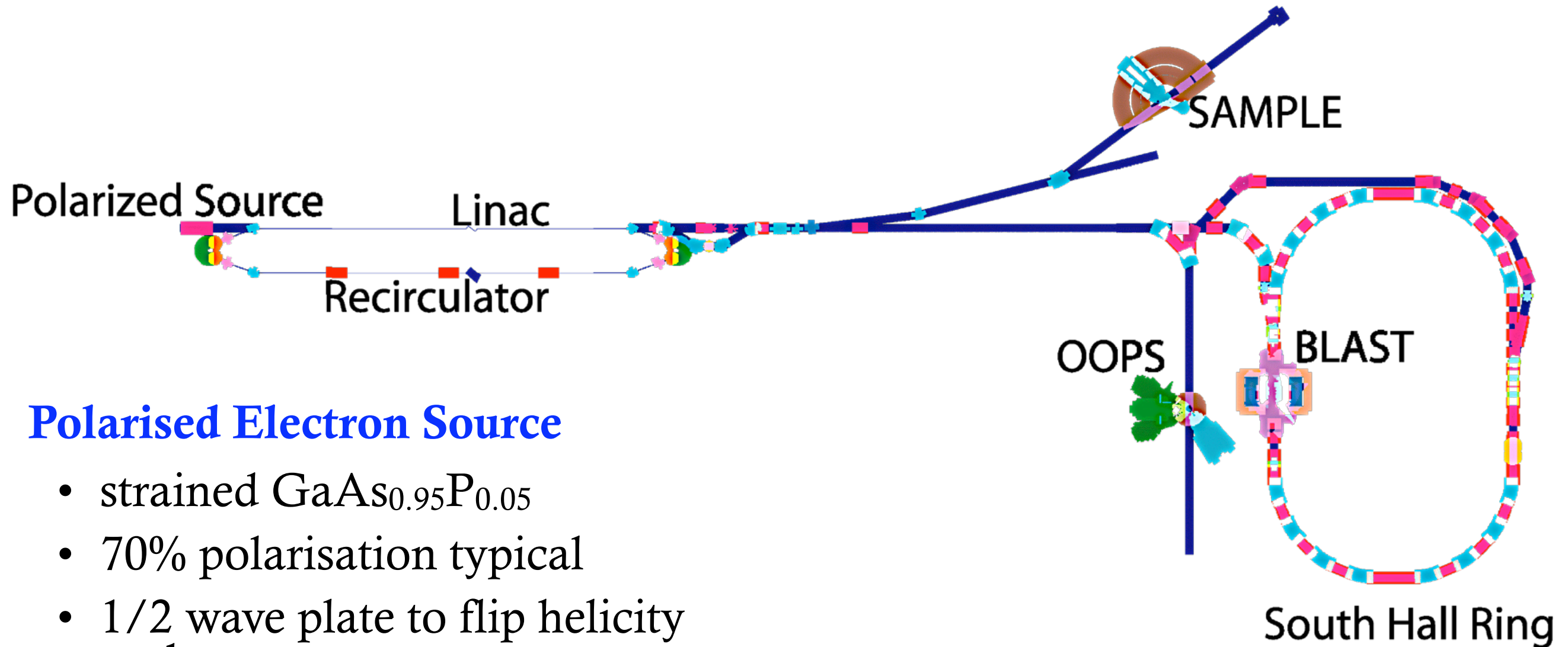
Highly polarized, internal gas target, isotopically pure H or D

- 6×10^{13} atoms/cm², 80% vector (H and D), 70% tensor (D) polarization

L/R Symmetric, large acceptance, general purpose detector

- 20°-80° polar, $\pm 15^\circ$ azimuthal, $0.1 < Q^2 < 0.8$ (GeV/c)²
- Simultaneous detection of $e^\pm$, $\pi^\pm$, p, n, d

MIT-Bates Linear Accelerator Center



Polarised Electron Source

- strained $\text{GaAs}_{0.95}\text{P}_{0.05}$
- 70% polarisation typical
- 1/2 wave plate to flip helicity each run

500 MeV Linac with recirculator

- polarised electrons up to 1 GeV

North and South Expt. Halls

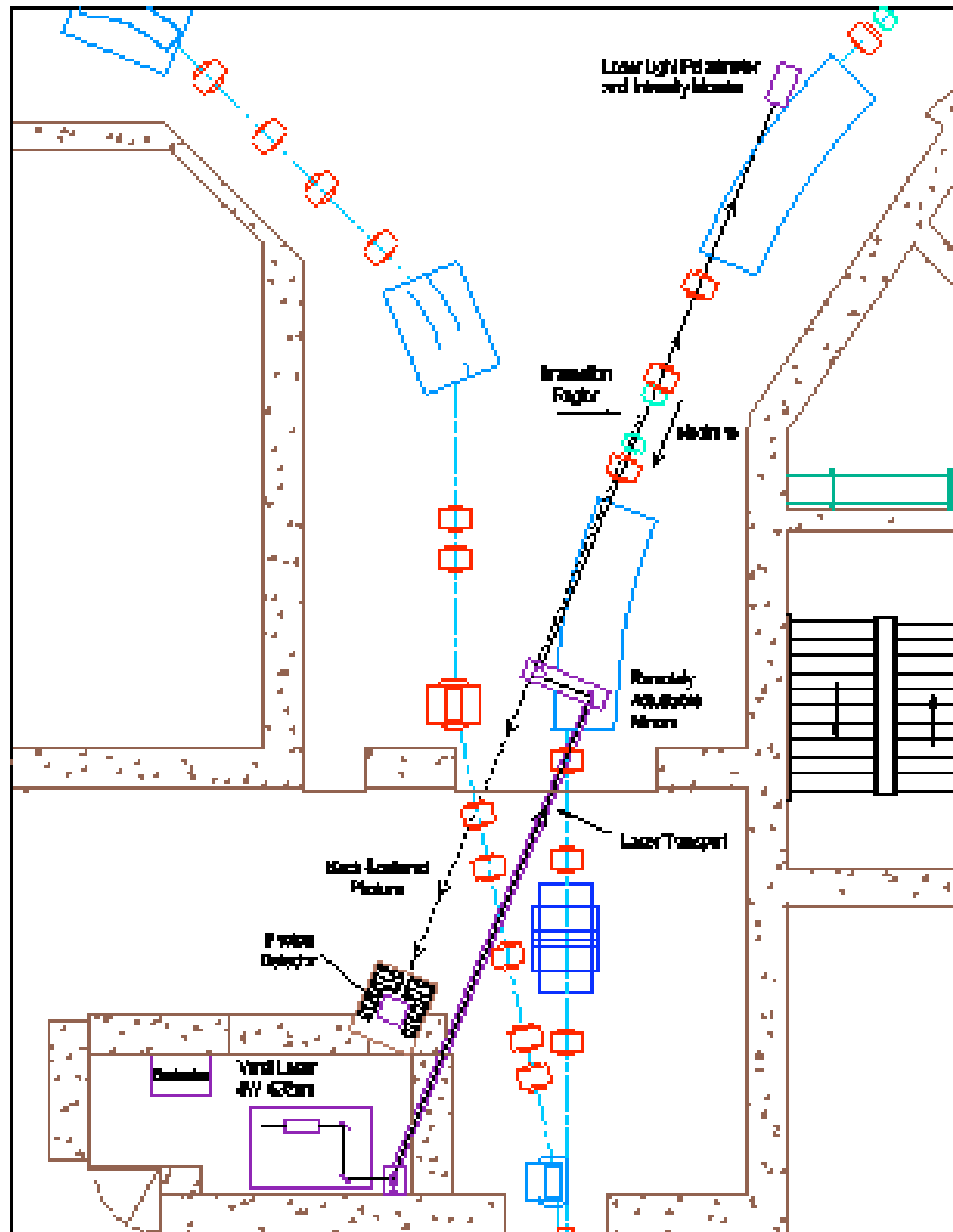
- SAMPLE - north hall
- OOPS/BLAST - south hall

South Hall Ring

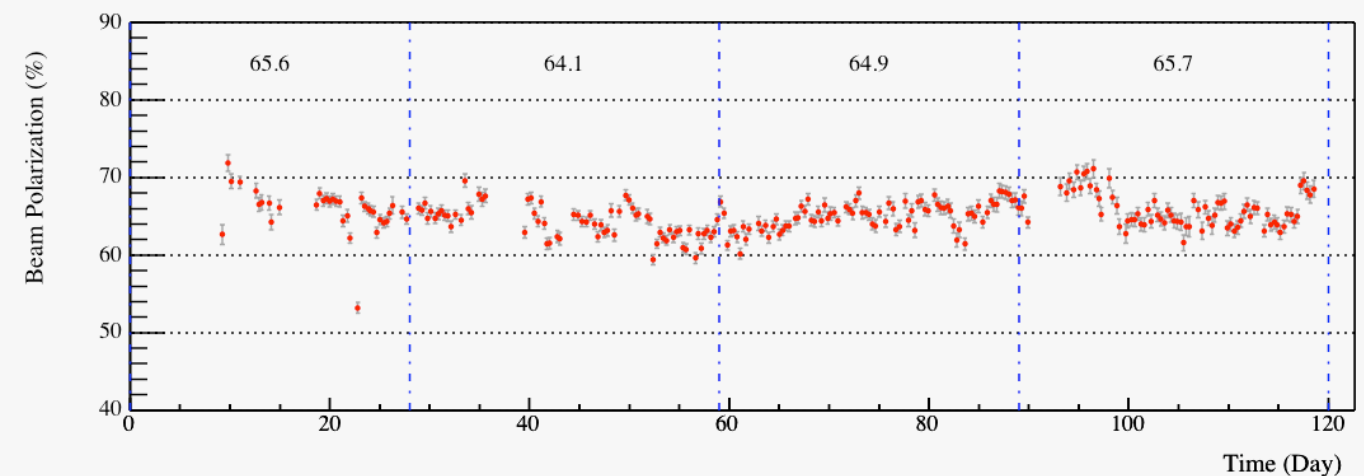
- stack to 225 mA typical
- 30 minute lifetime
- 65 % polarisation typical
- Siberian snake maintains longitudinal spin at target

Compton Polarimeter

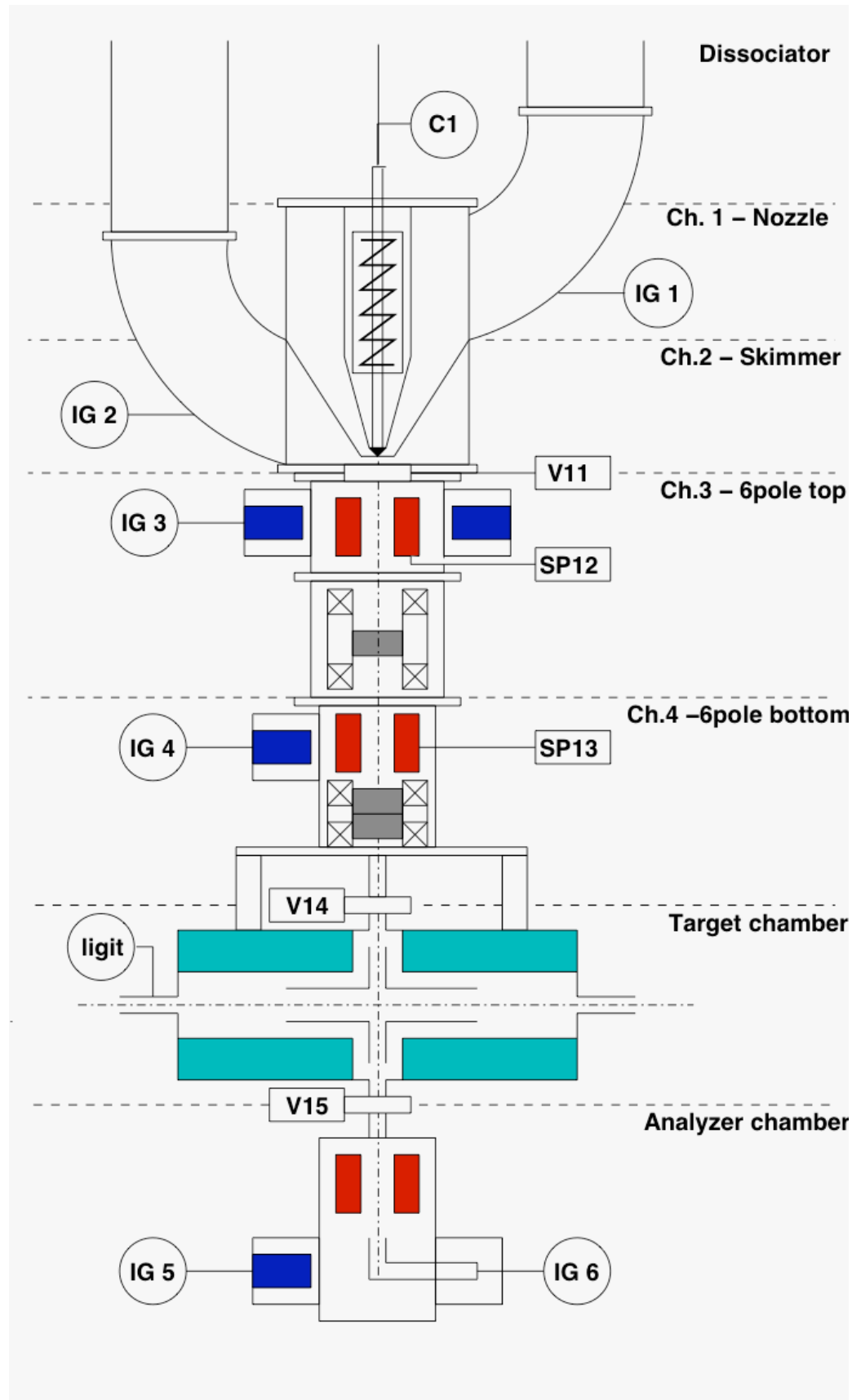
Monitor beam polarisation in ring



- 5 W laser, 532 nm, circularly polarised incident on oncoming electron beam
- Backscattered photons detected in CsI
- Laser helicity flipped in Pockels cell
- Asymmetry yields beam polarisation
- Chopper wheel allows simultaneous measure of background
- Typical beam polarisation 65 %
- Systematic uncertainty <3%



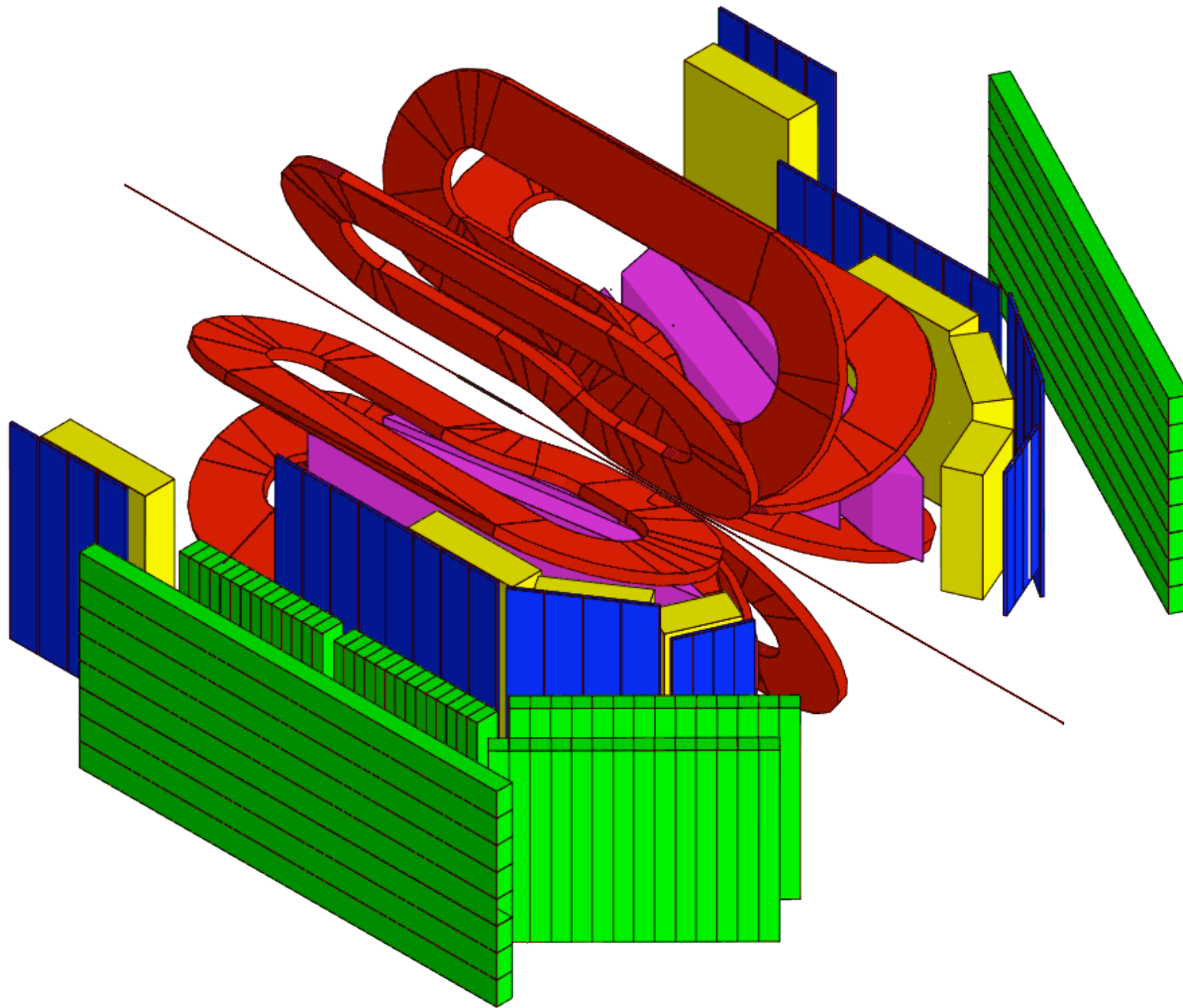
Internal, Polarised Gas Target



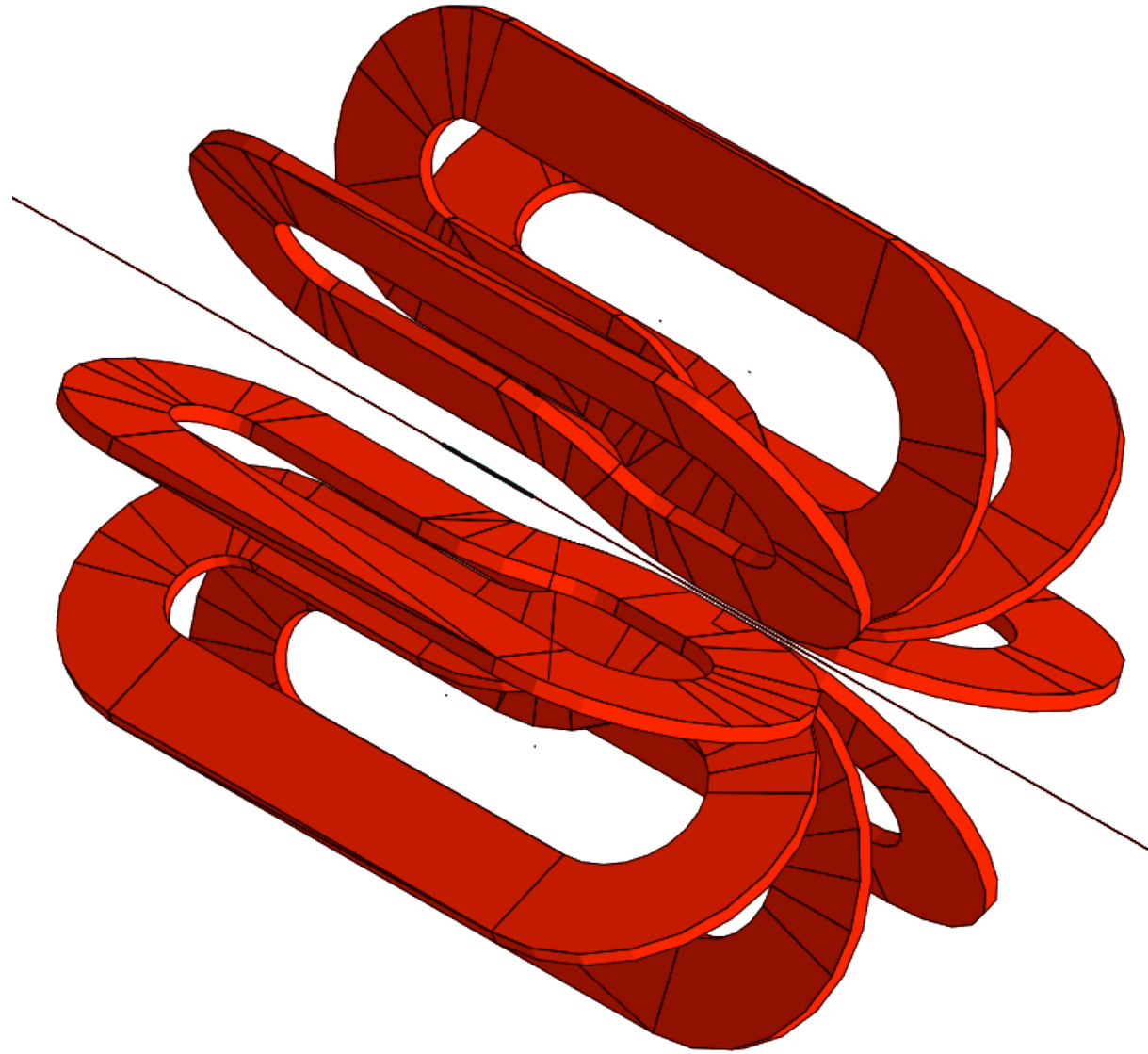
Atomic Beam Source

- series of focusing magnets and RF transition units populate and transport the desired spin state to the target cell
- target cell - thin walled, open ended tube, 60 cm long, $\varnothing 15$ mm
- isotopically pure ^1H or ^2H
- vector polarised ^1H
- vector and tensor polarised ^2H
- randomly change spin state every 5' during run
- target density 6×10^{13} atoms/cm²
- vector polarisation 80 % typical
- tensor polarisation 68 % typical

BLAST Detector



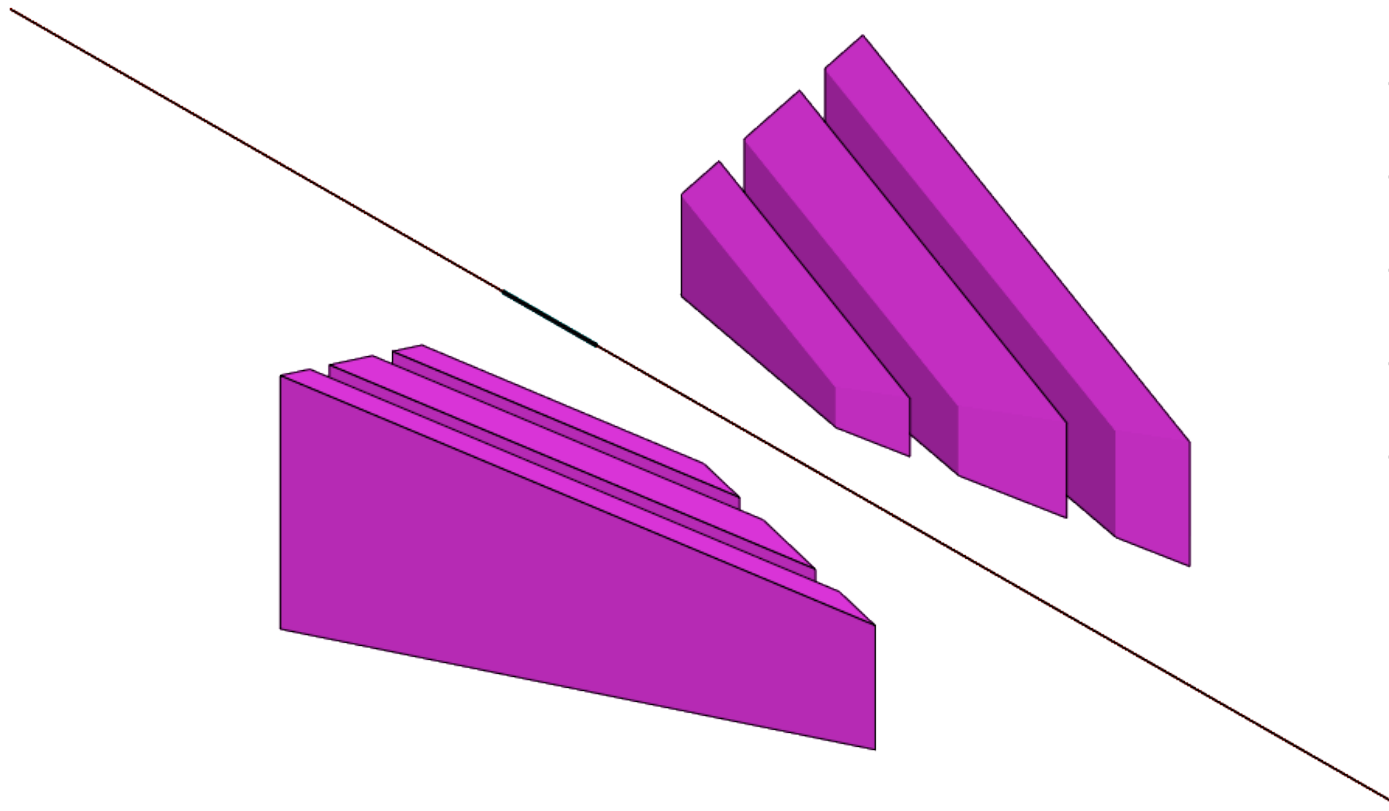
BLAST Detector



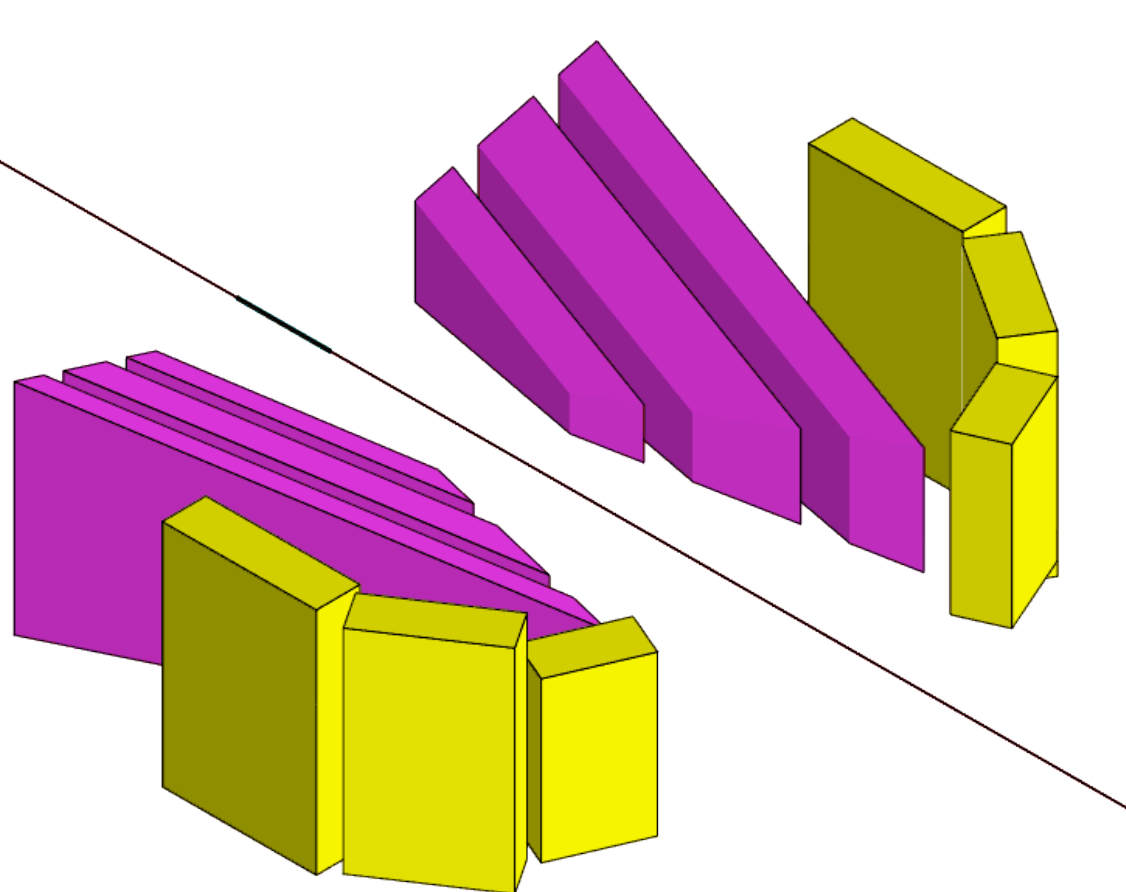
- 8 sector toroid magnet
 - minimise effect on beam and target polarisation
- 3.8 kG maximum field
- two horizontal sectors instrumented

BLAST Detector

- 3 wire chambers / sector
 - single gas volume
- 2 superlayers / chamber
 - +/- 10° stereo
- 3 sense layers / superlayer
- total 18 layers of tracking
- momentum analysis
- scattering angles
- event vertex
- particle charge

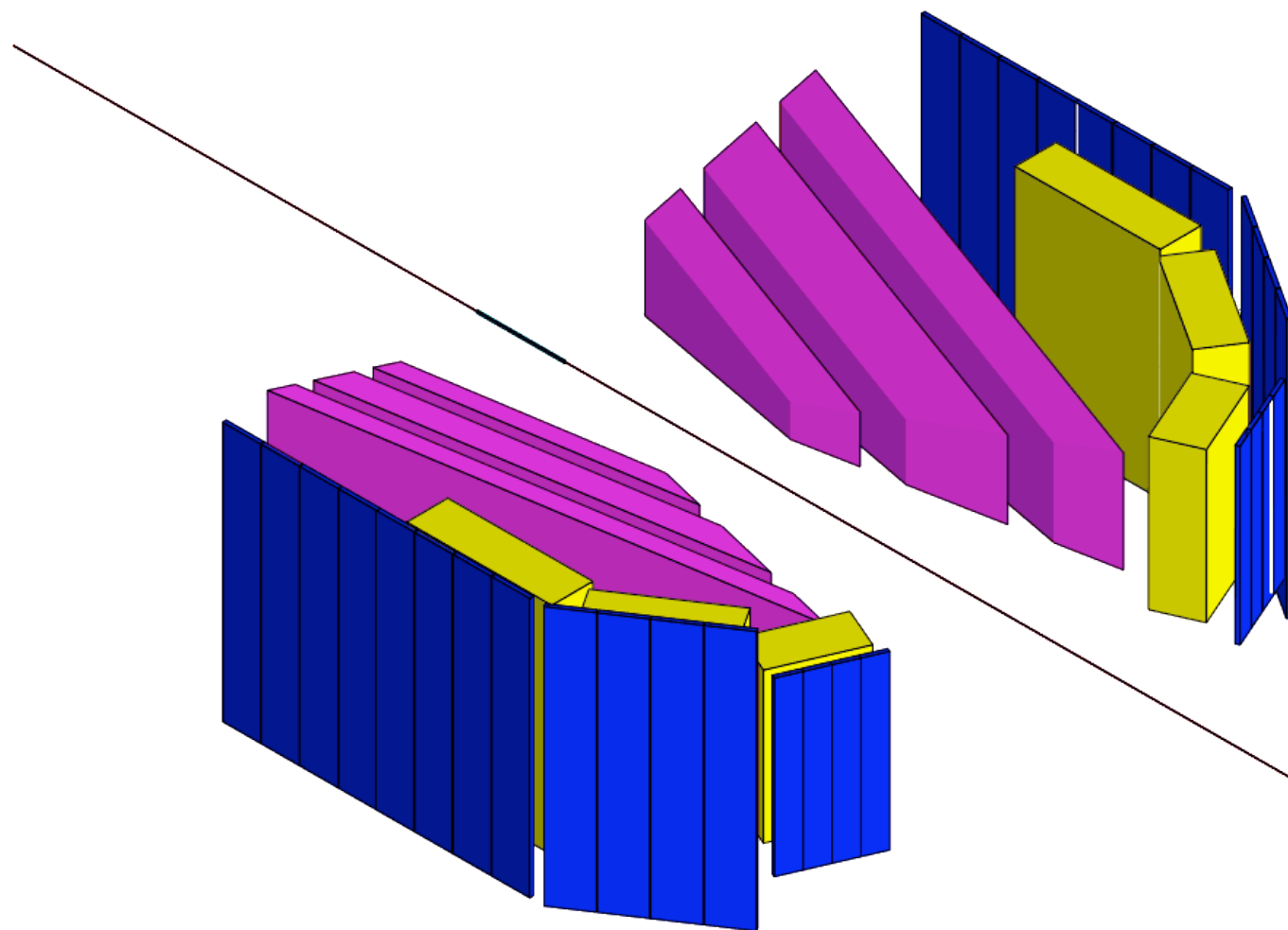


BLAST Detector



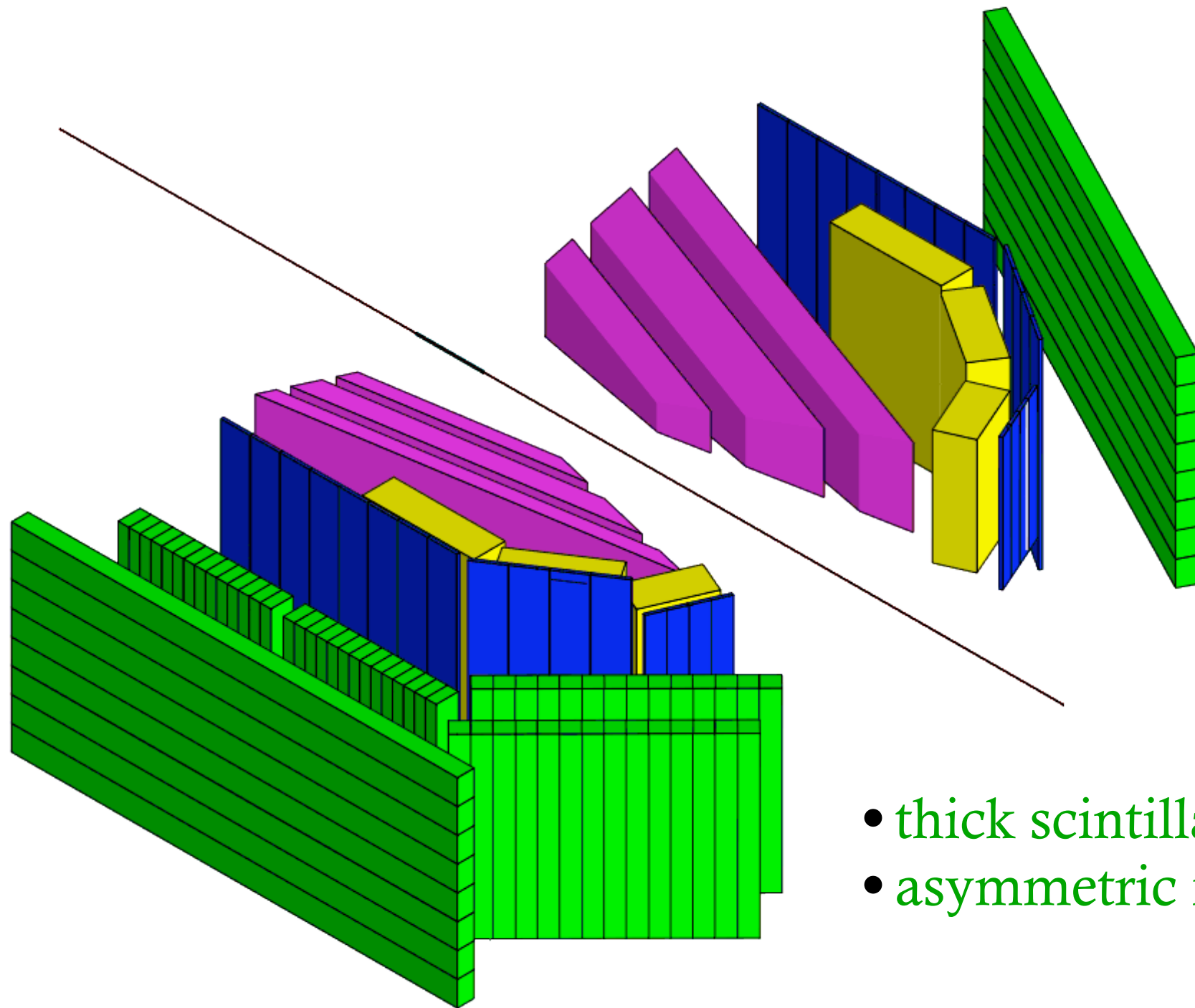
- Aerogel Cerenkov
- pion / electron separation

BLAST Detector



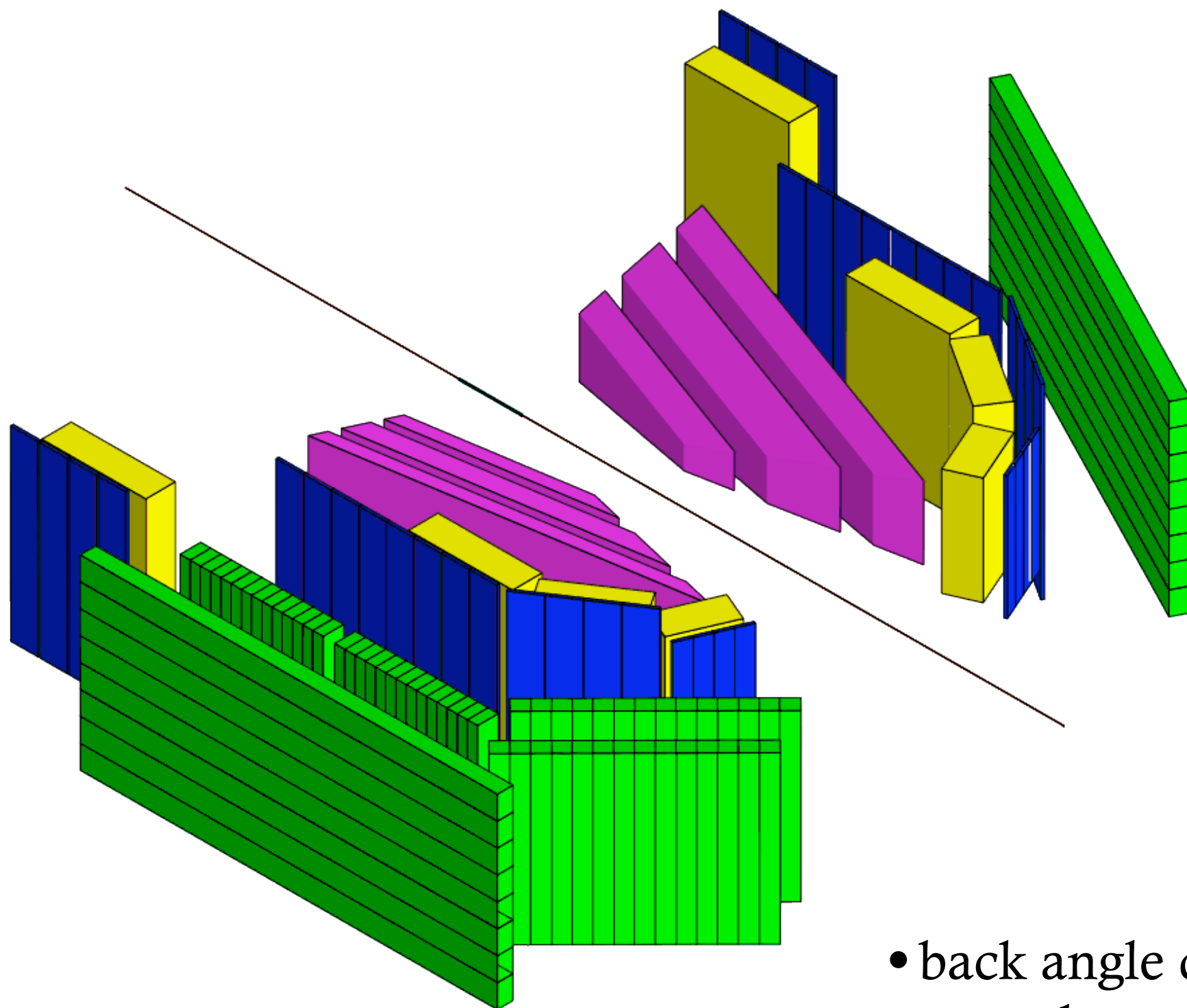
- time of flight scintillator walls
- relative timing
- trigger timing

BLAST Detector



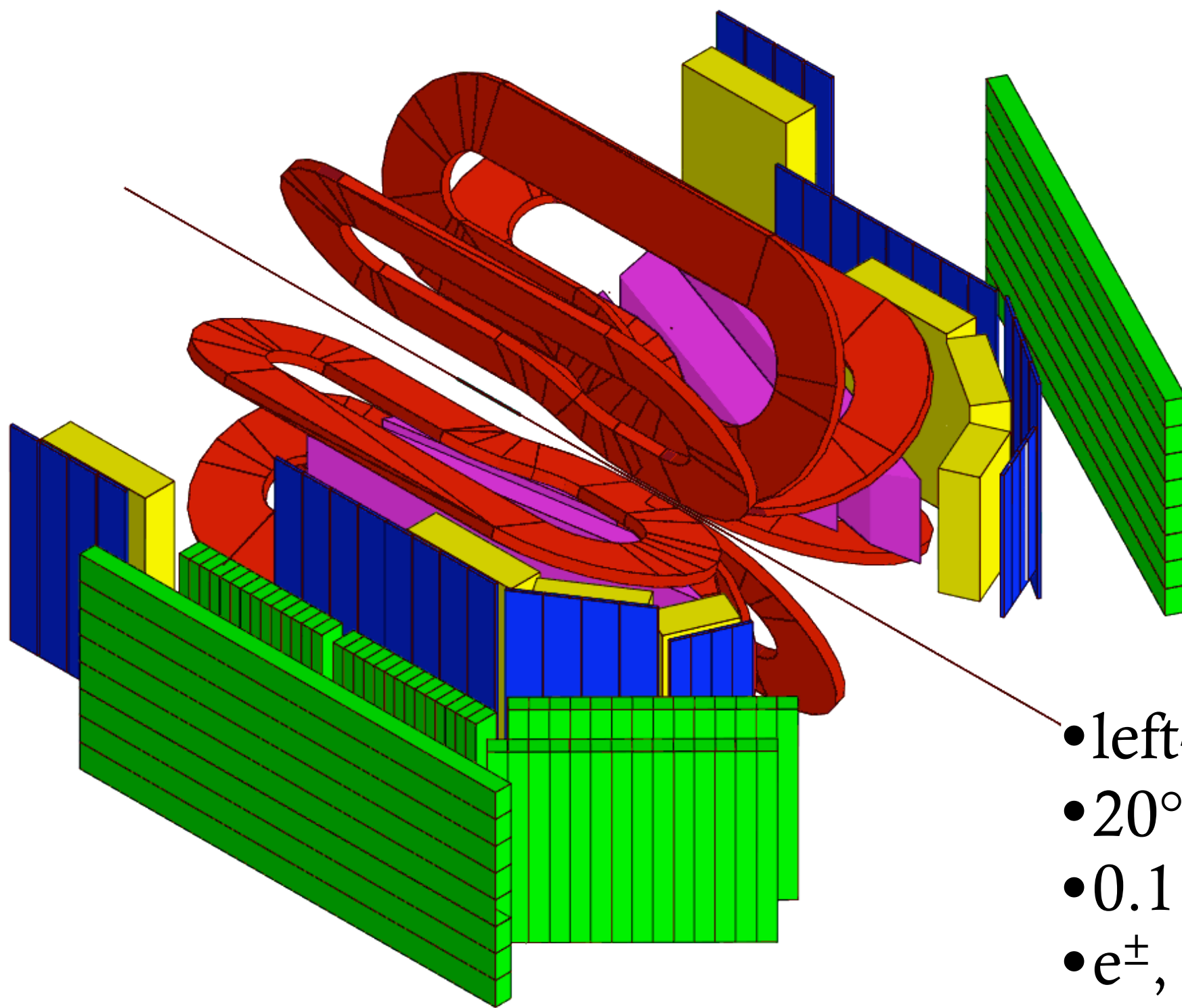
- thick scintillators for neutron detector
- asymmetric favouring right sector

BLAST Detector



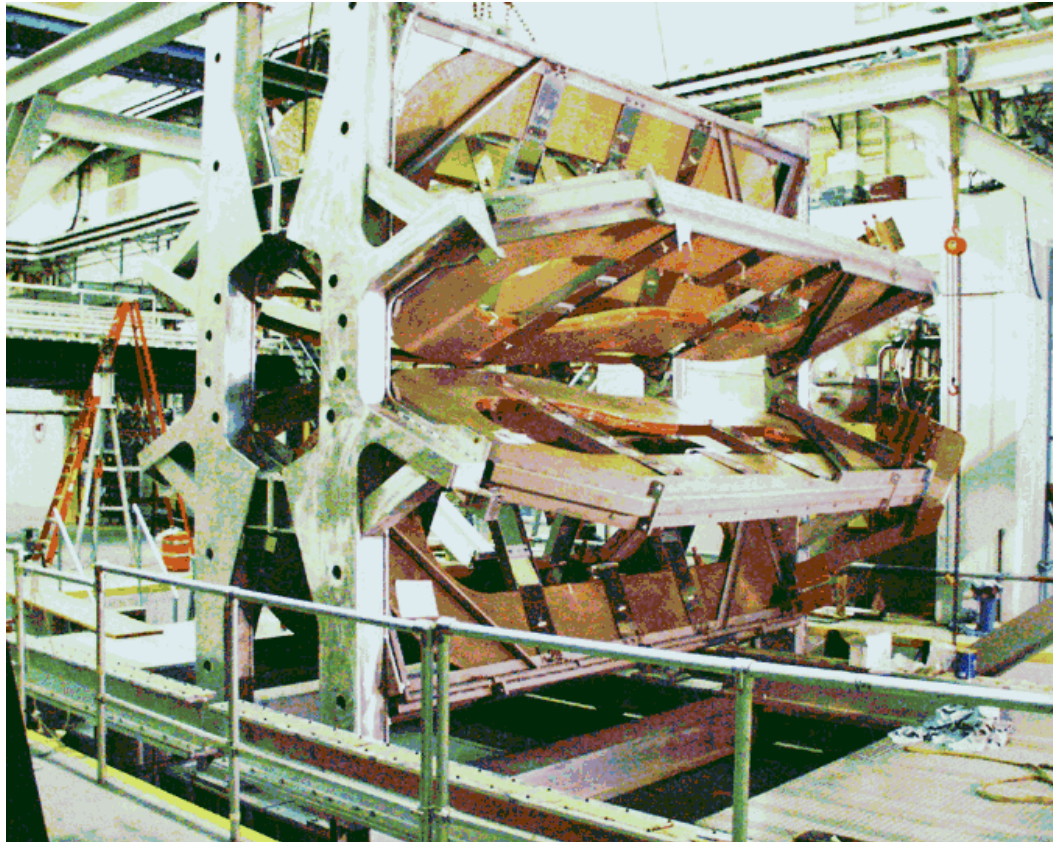
- back angle detectors
- extend coverage, no tracking

BLAST Detector

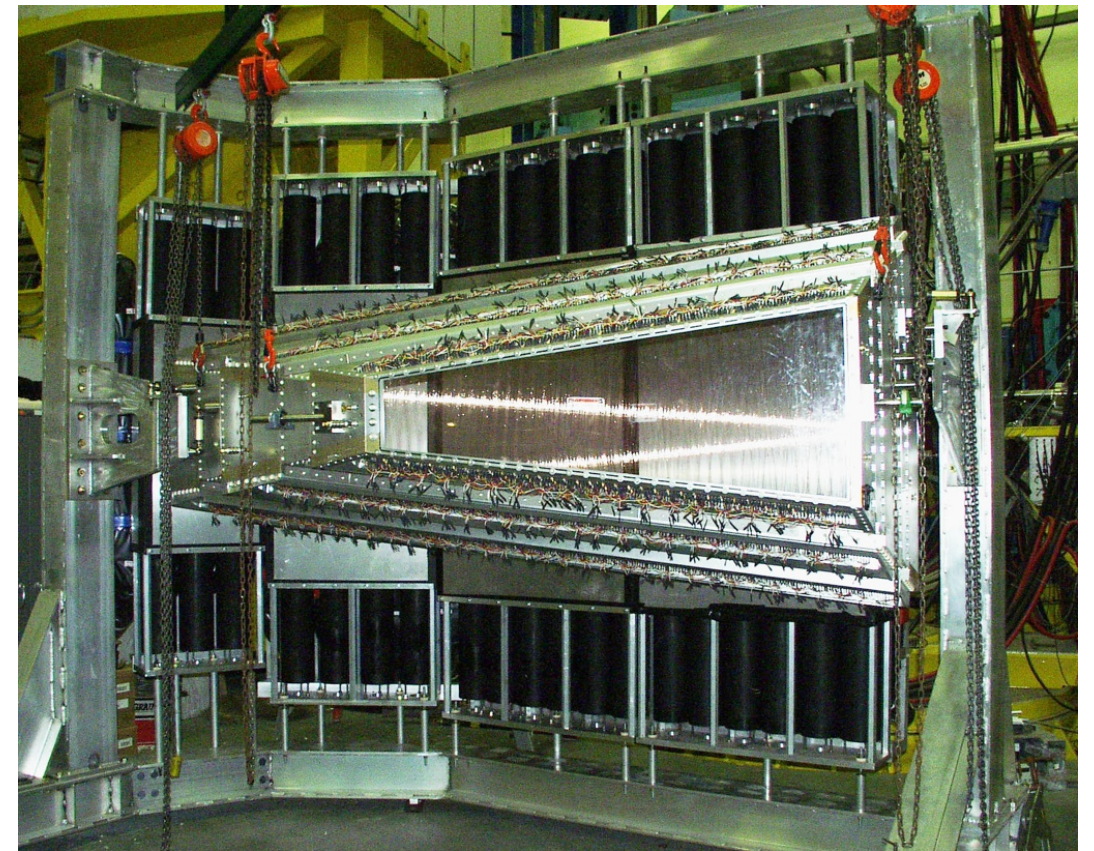


- left-right symmetric
- $20^\circ - 80^\circ \theta$, $\pm 15^\circ \varphi$
- $0.1 < Q^2 < 0.8 \text{ (GeV/c)}^2$
- $e^\pm$, p, n, d, $\pi^\pm$

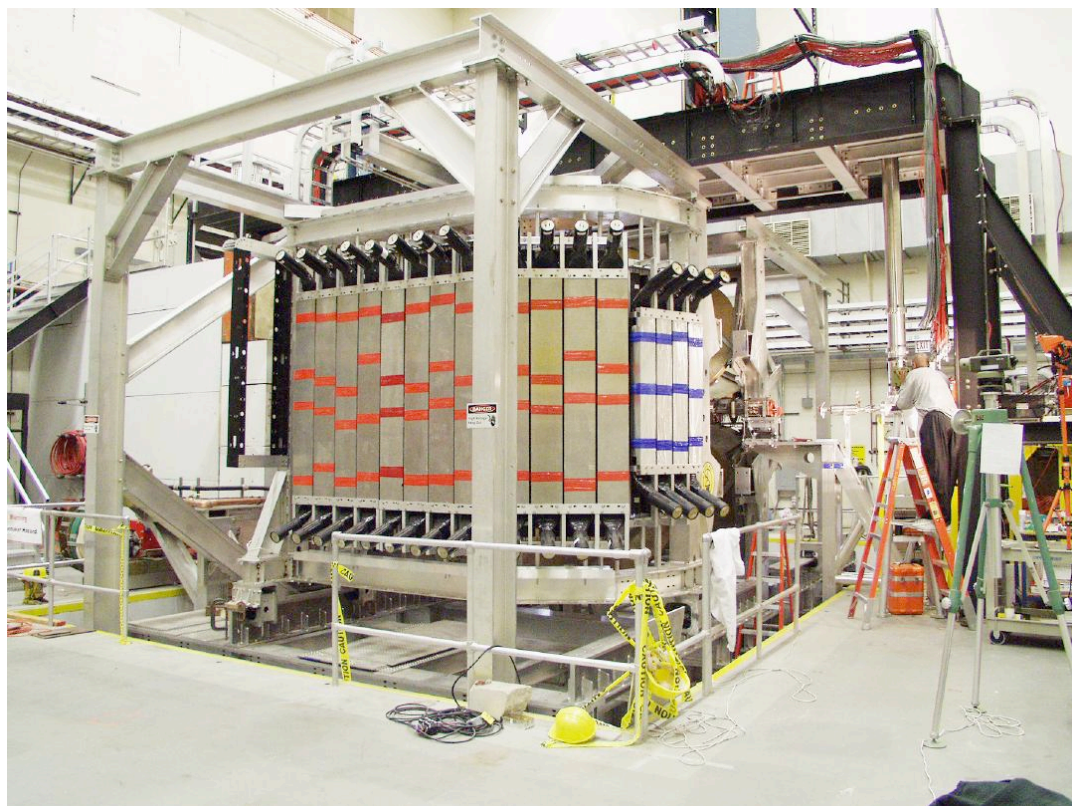
BLAST Detector Components



Bates



MIT



UNH



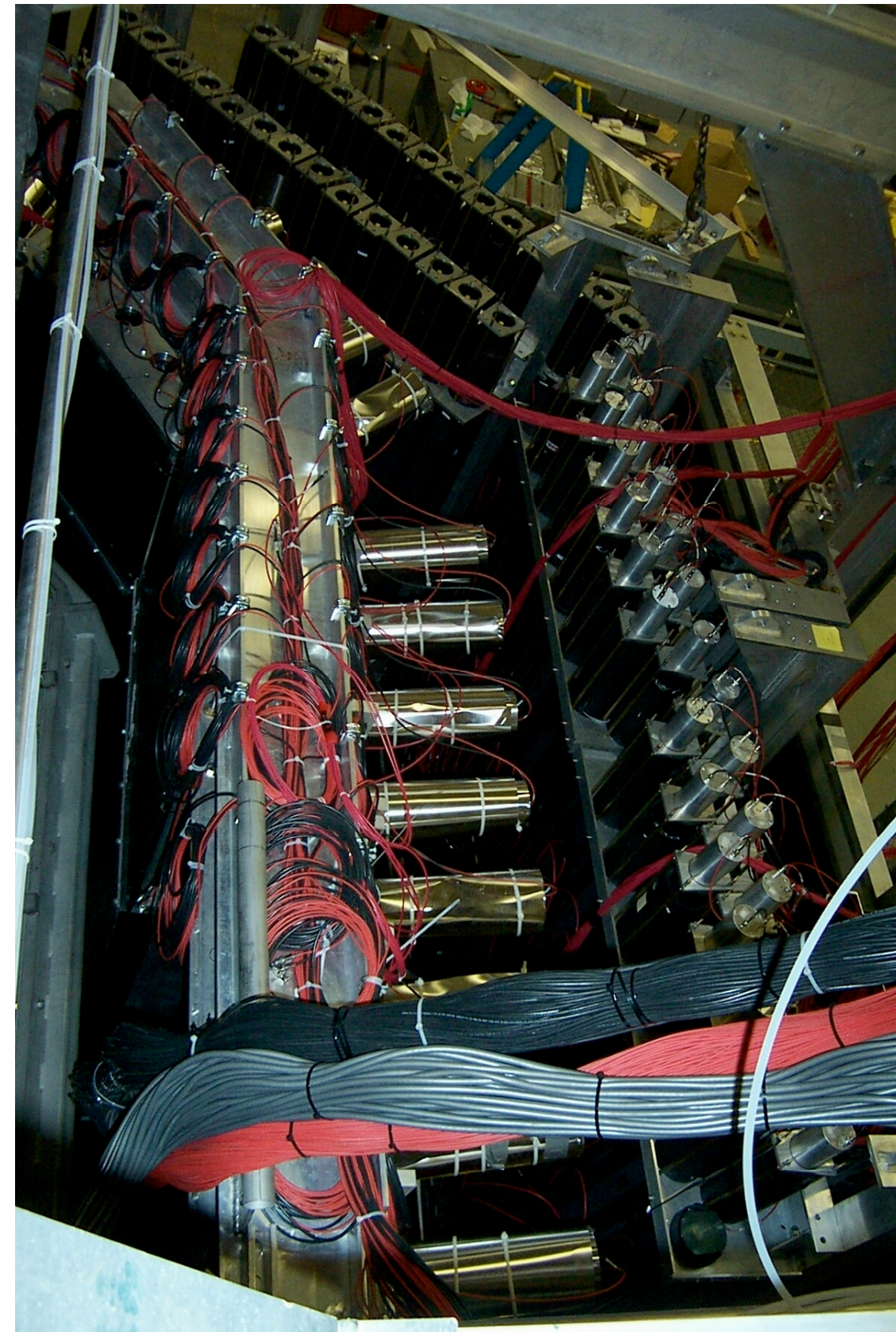
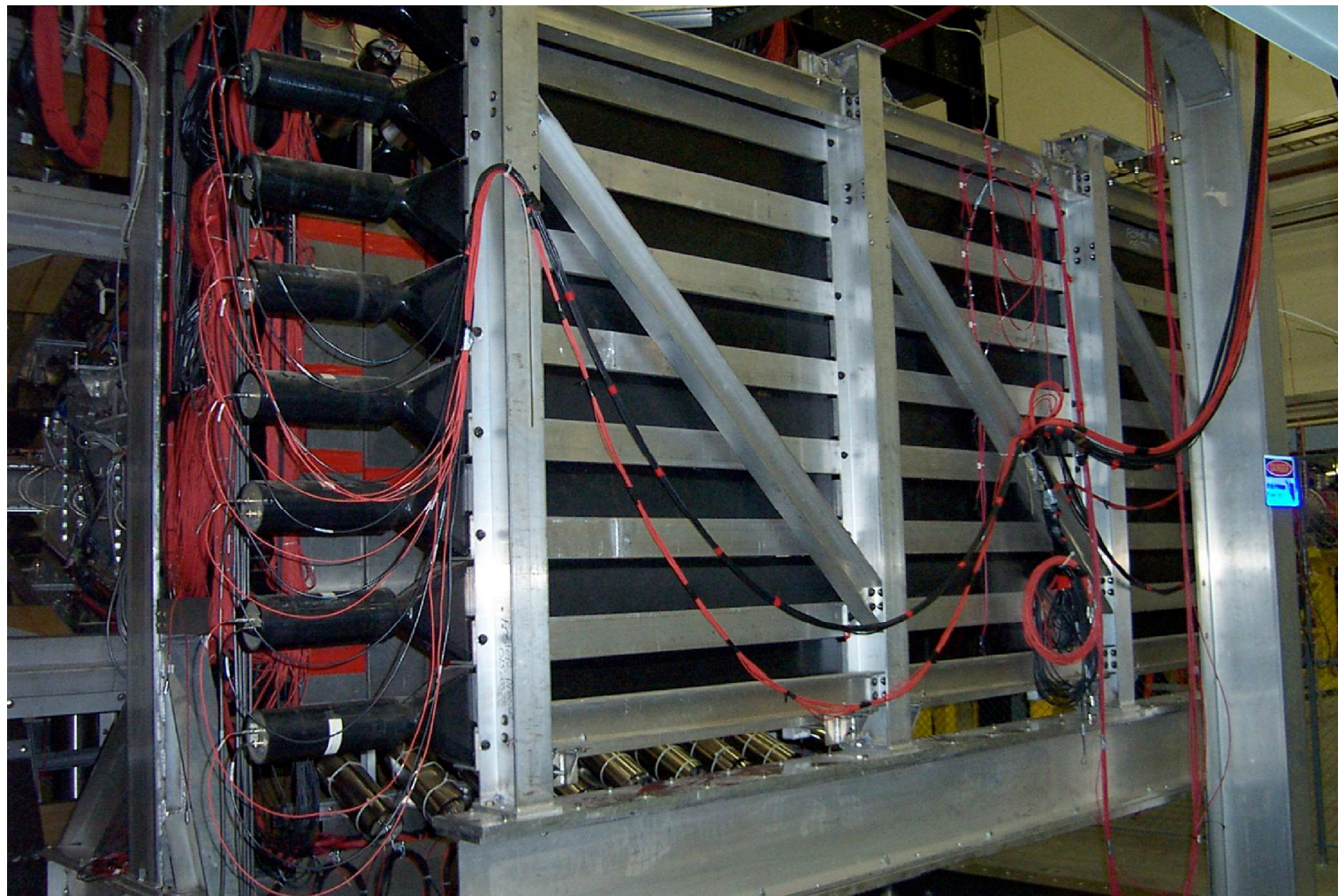
ASU

BLAST Detector Components

Neutron Detectors

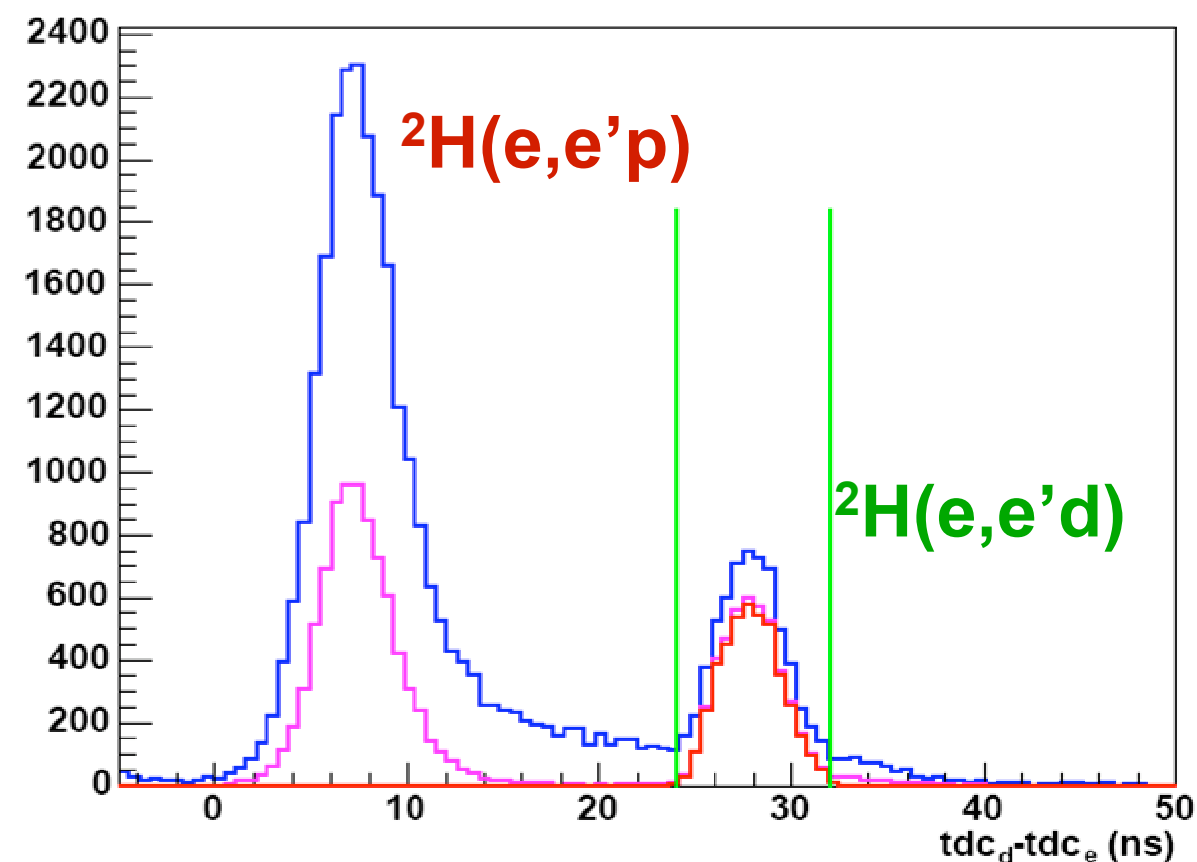
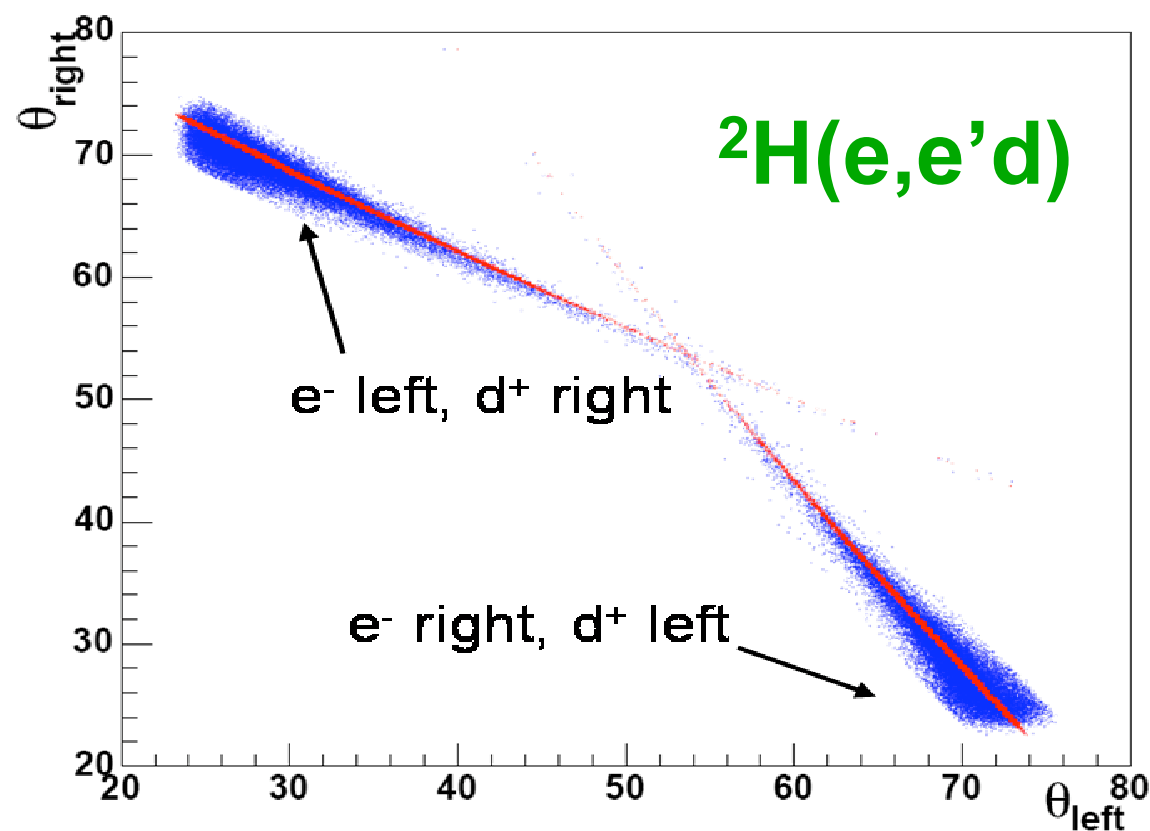
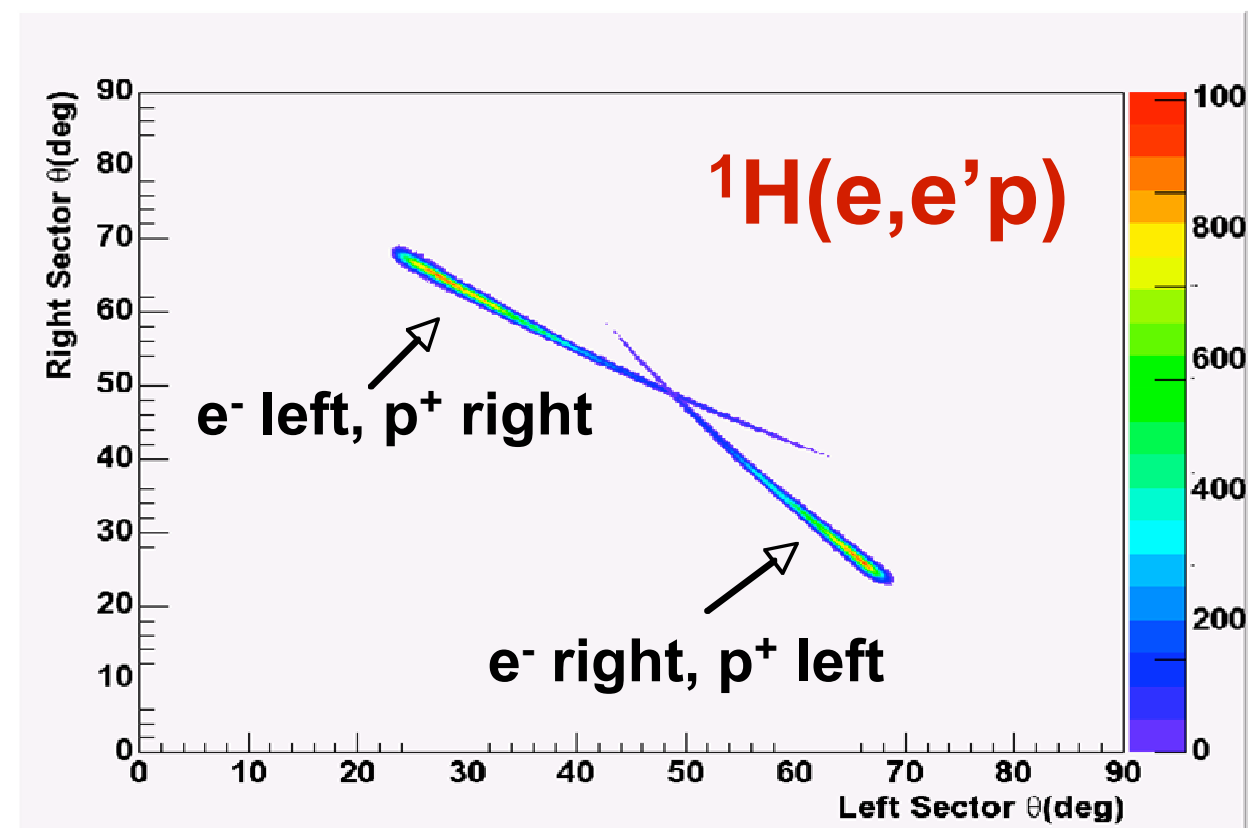
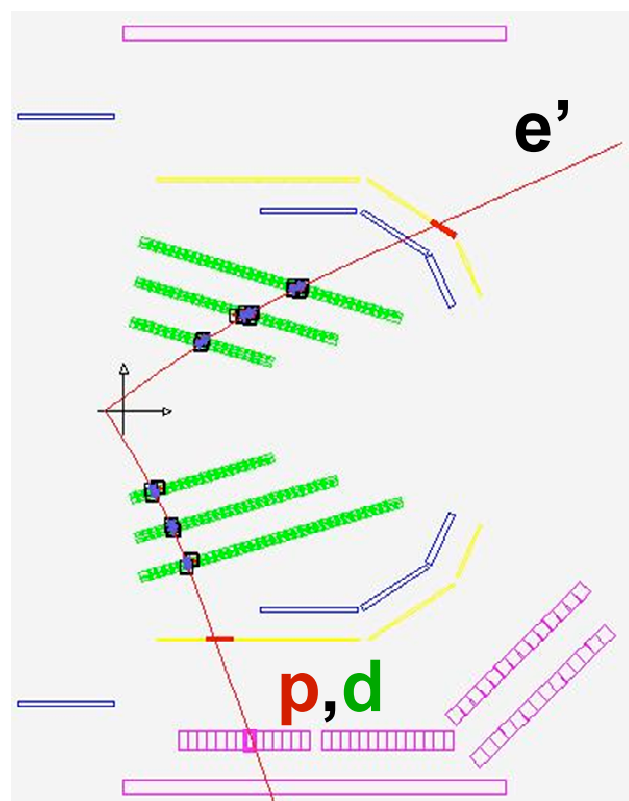
MIT

Ohio University



Event Selection

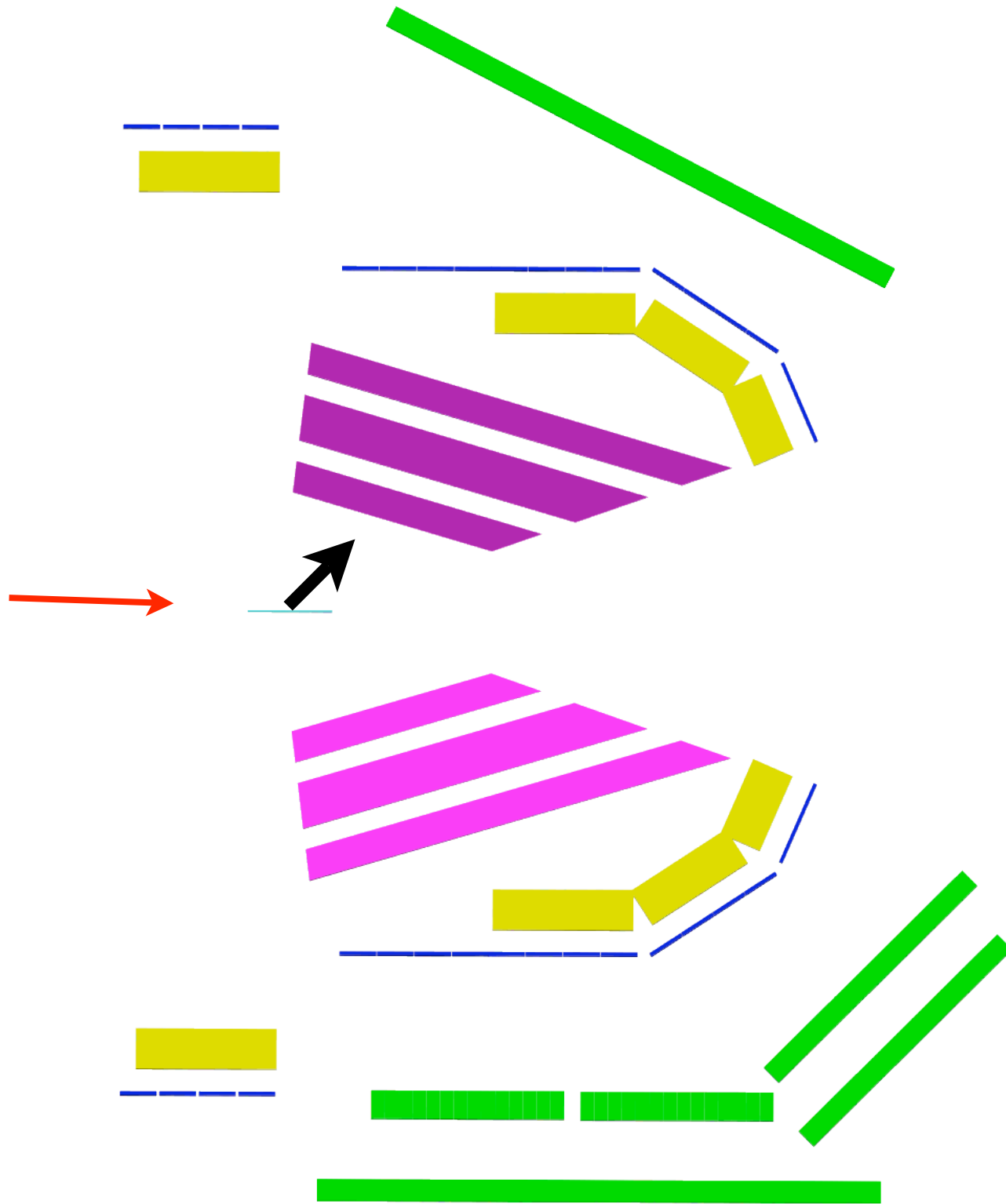
Charge+/-
Coplanarity
Kinematics
Timing



Orientation of Target Spin

Target spin angle

- 32° (2004) / 45° (2005)
- horizontal into the left sector



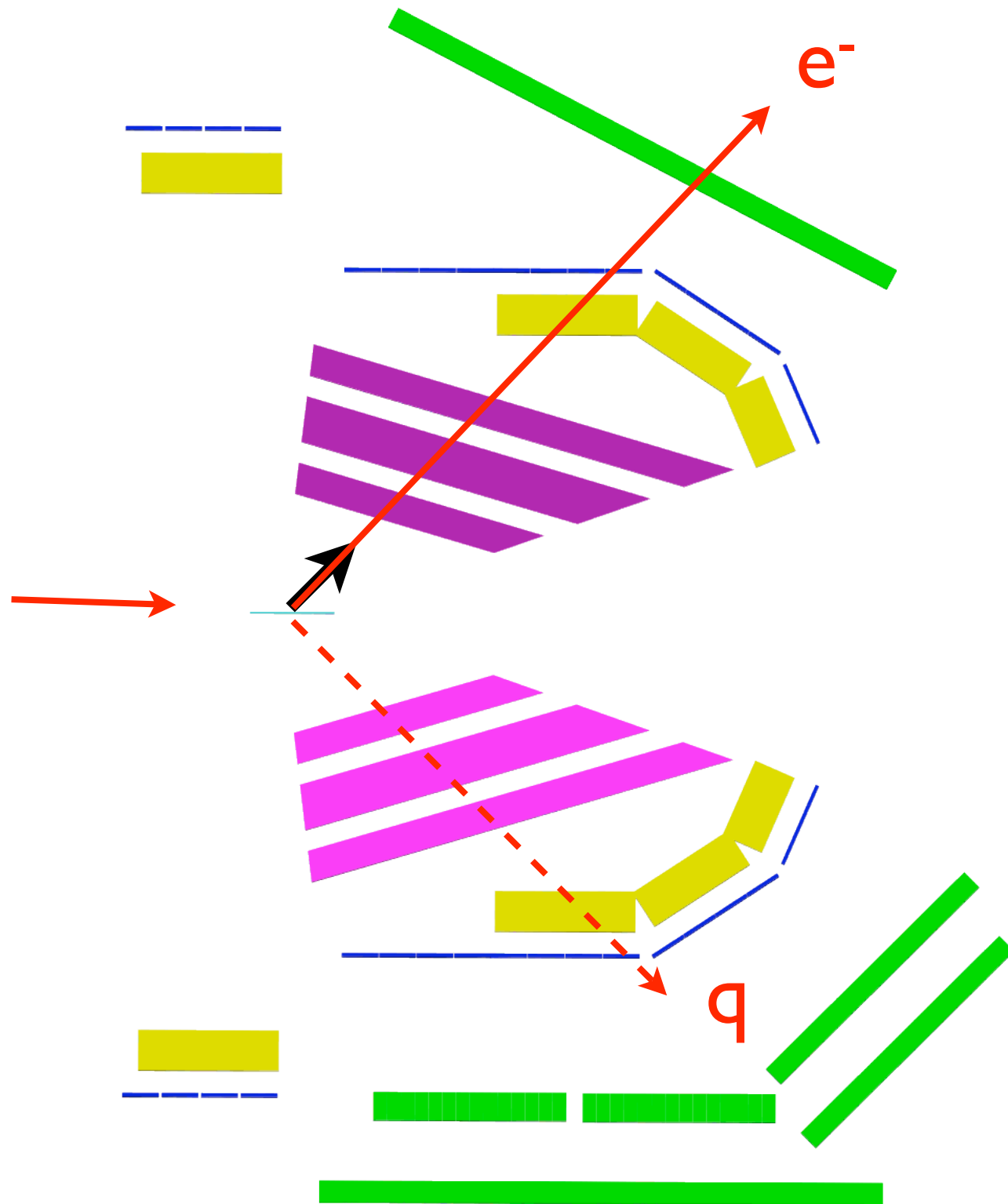
Orientation of Target Spin

Target spin angle

- 32° (2004) / 45° (2005)
- horizontal into the left sector

Electron scatters to left sector

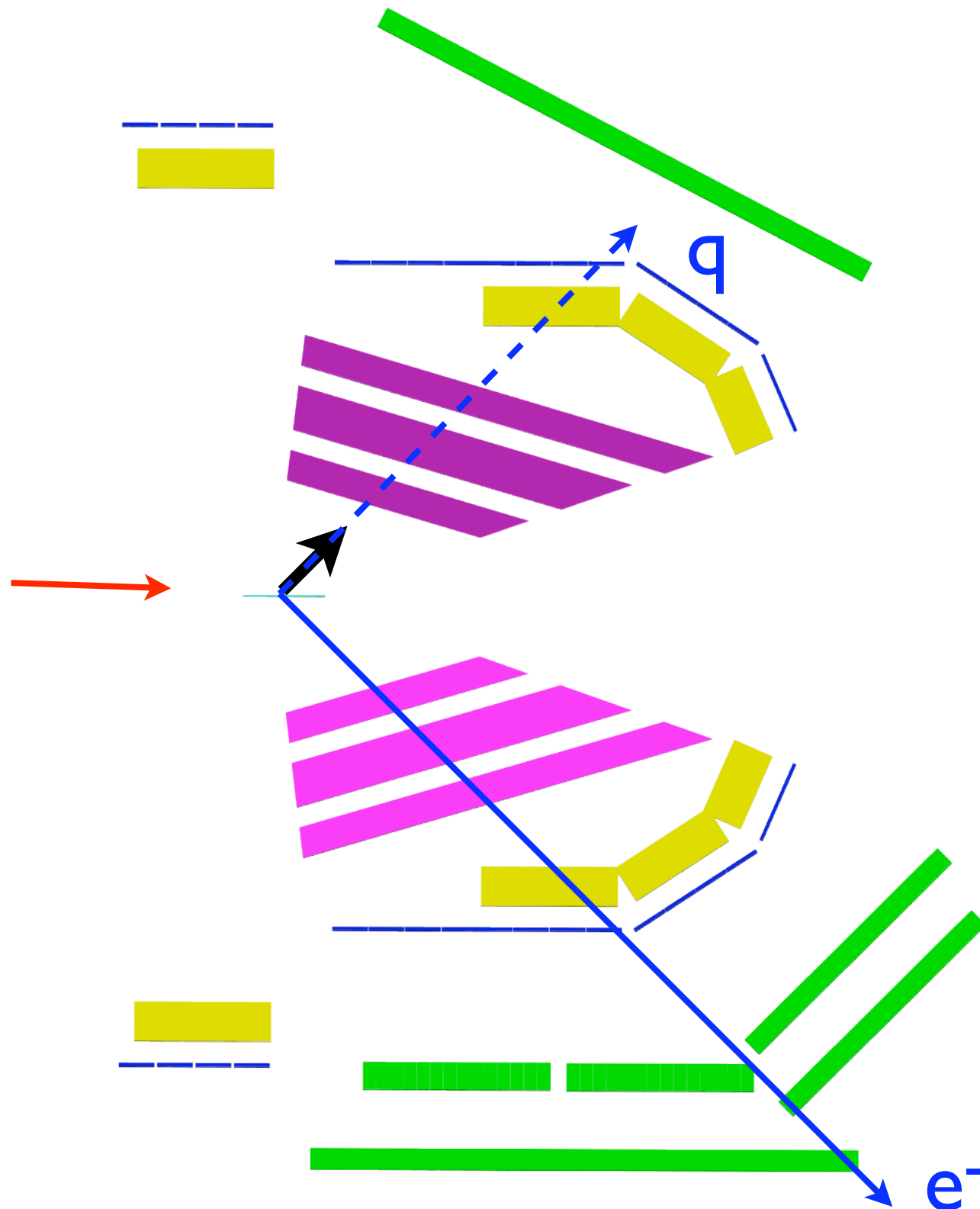
- $q \approx$ perpendicular to target spin
- $\theta^* \approx 90^\circ$
- “spin perpendicular” kinematics



Orientation of Target Spin

Target spin angle

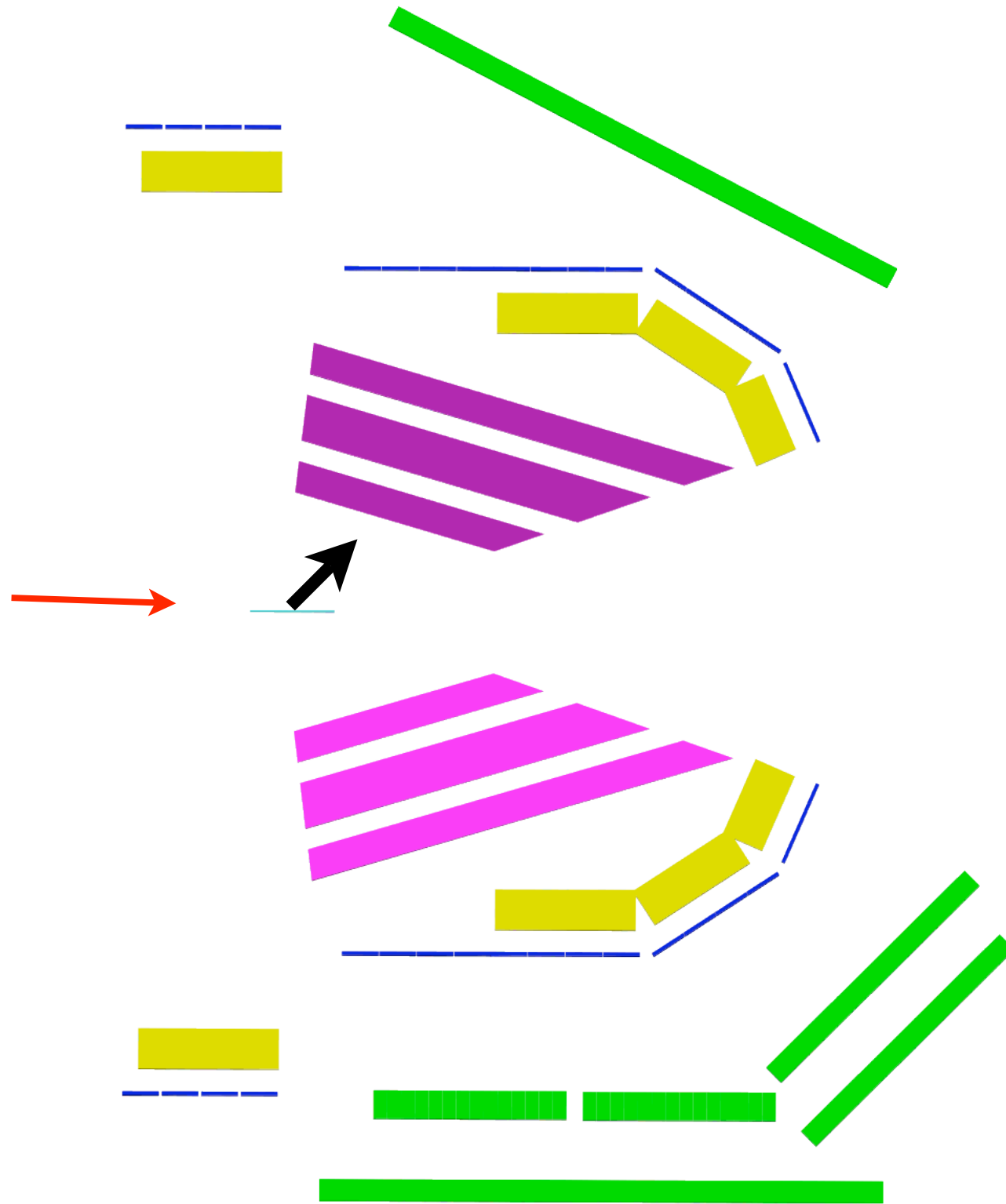
- 32° (2004) / 45° (2005)
- horizontal into the left sector



Electron scatters to right sector

- $q \approx$ parallel to target spin
- $\theta^* \approx 0^\circ$
- “spin parallel” kinematics

Orientation of Target Spin



Target spin angle

- 32° (2004) / 45° (2005)
- horizontal into the left sector

Electron scatters to left sector

- $q \approx$ perpendicular to target spin
- $\theta^* \approx 90^\circ$
- “spin perpendicular” kinematics

Electron scatters to right sector

- $q \approx$ parallel to target spin
- $\theta^* \approx 0^\circ$
- “spin parallel” kinematics

BLAST Physics

Polarised Hydrogen

$$^1\vec{H}(\vec{e}, e') \quad ^1\vec{H}(\vec{e}, e'p) \quad ^1\vec{H}(\vec{e}, e'p)\gamma, \pi^0 \quad ^1\vec{H}(\vec{e}, e'\pi^+)n \quad ^1\vec{H}(\vec{e}, e'\pi^+n)$$

Inclusive **G^p_E/G^p_M** **$N-\Delta$: EMR, CMR** **Photoprod.**

Vector Polarised Deuterium

$$^2\vec{H}(\vec{e}, e') \quad ^2\vec{H}(\vec{e}, e'd) \quad ^2\vec{H}(\vec{e}, e'p)n \quad ^2\vec{H}(\vec{e}, e'n)p \quad ^2\vec{H}(\vec{e}, e'\pi^{\pm,0})$$

G^n_M **$T^e_{11} : G^d_M$** **$A^v_{ed} : L=2$** **G^n_E** **$N-\Delta$**

Tensor Polarised Deuterium

$$^2\overleftrightarrow{H}(e, e'd) \quad ^2\overleftrightarrow{H}(e, e'p)n \quad ^2\overleftrightarrow{H}(e, e'n)p \quad ^2\overleftrightarrow{H}(\gamma, pn) \quad ^2\overleftrightarrow{H}(\vec{e}, e'\pi^{\pm})$$

$T_{20} : G^d_Q$ **$A^T_d : L=2$** **photodisint.** **1S_0**

Elastic Scattering from Hydrogen

With polarized beam and target can measure asymmetries

$$A_{exp} = P_b P_t \frac{-2\tau v_{T'} \cos \theta^* G_M^p{}^2 + 2\sqrt{2\tau(1+\tau)} v_{TL'} \sin \theta^* \cos \phi^* G_M^p G_E^p}{(1+\tau) v_l G_E^p{}^2 + 2\tau v_T G_M^p{}^2}$$

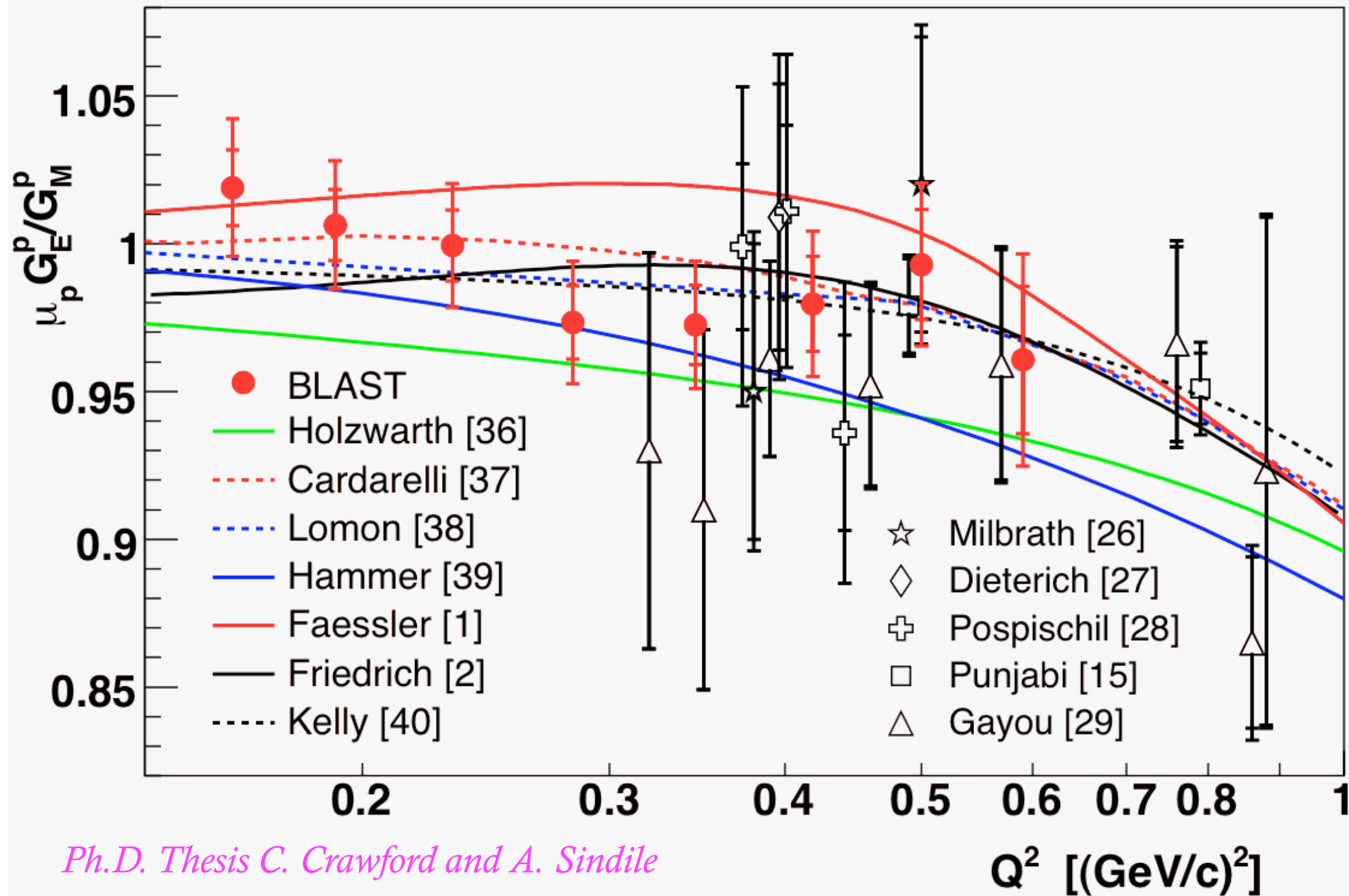
- note some terms vanish in perpendicular or parallel kinematics

With symmetric detector can form ratio of left/right asymmetries

$$R_A = \frac{A_L}{A_R} = \frac{z_L^* - x_L^* G_E^p / G_M^p}{z_R^* - x_R^* G_E^p / G_M^p}$$

- beam and target polarisations cancel
- all that remains is kinematic terms

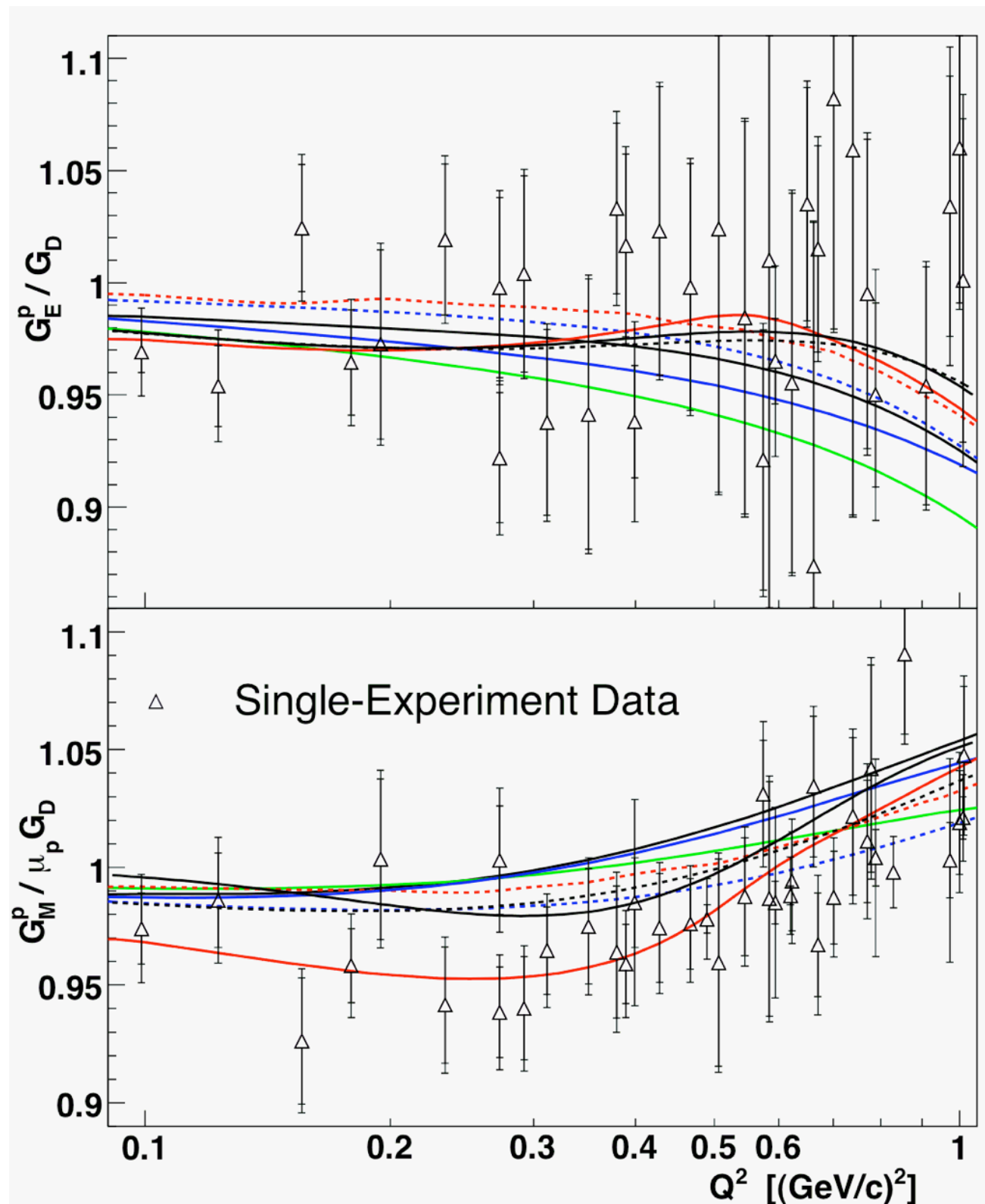
Ratio of Proton Elastic Form Factors



Impact of BLAST Results on World Data

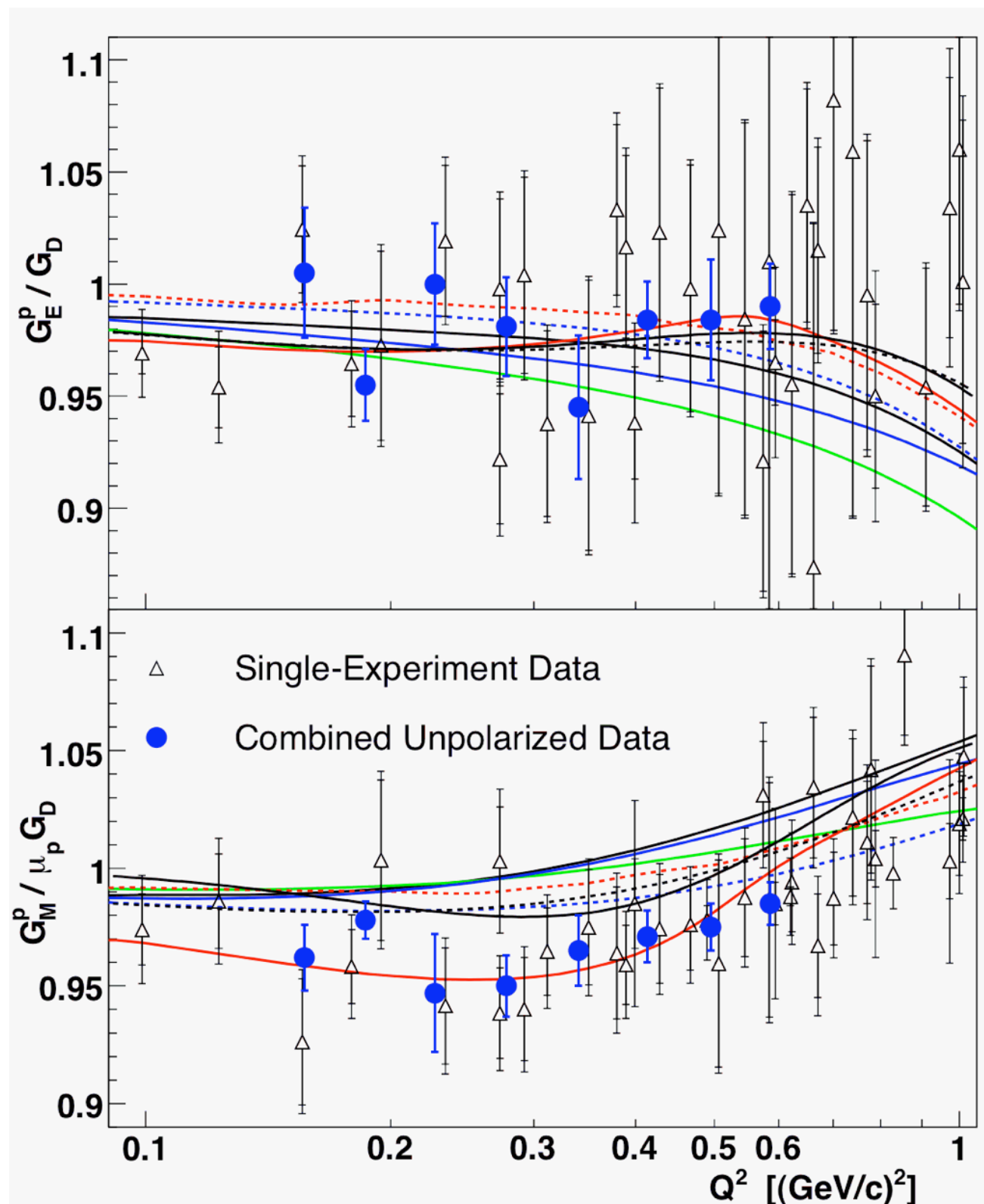
Proton elastic form factors

- G_E^p and G_M^p
- divided by dipole
- collection of unpolarised data



Ph.D. Thesis C. Crawford and A. Sindile

Impact of BLAST Results on World Data



Proton elastic form factors

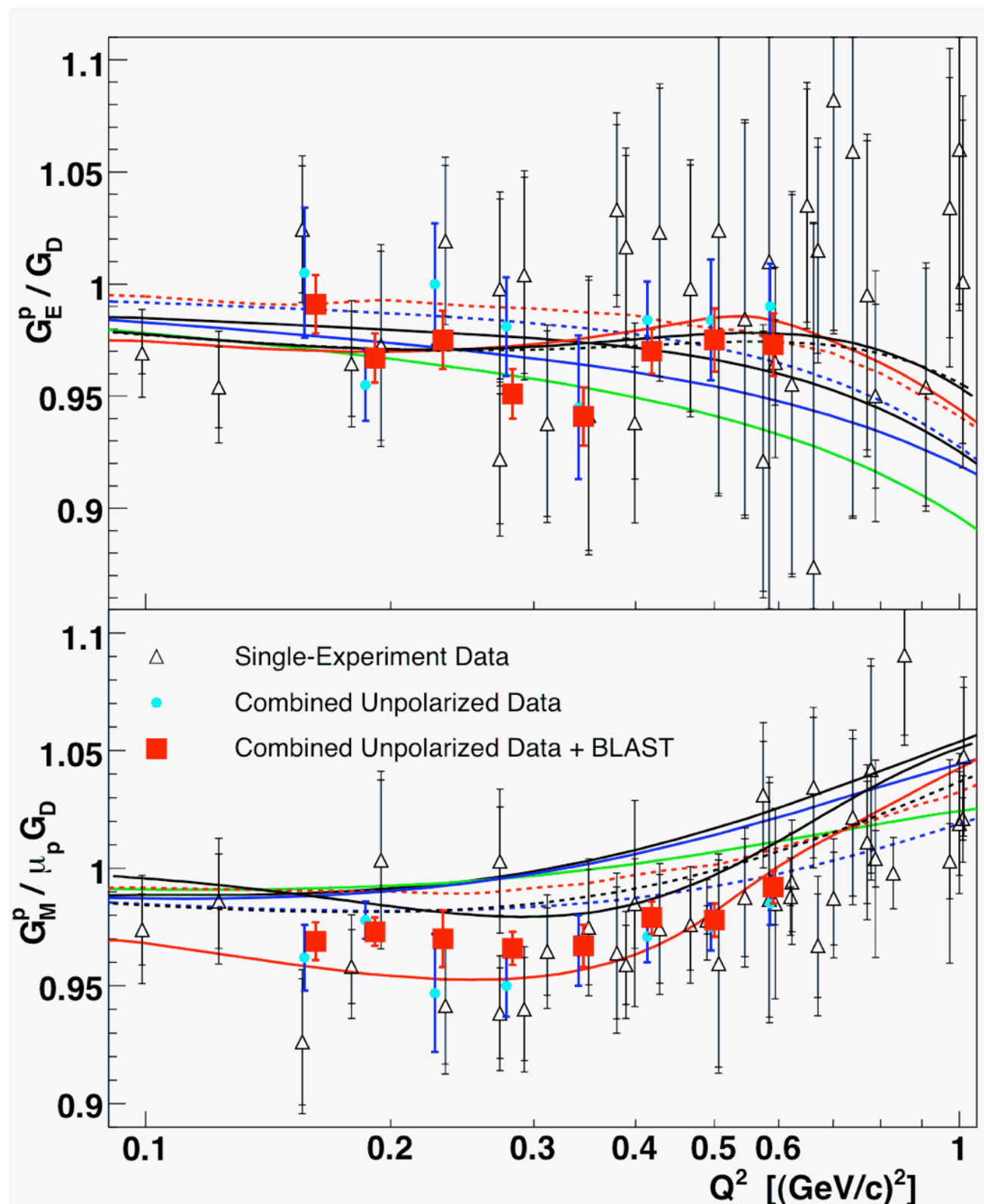
- G_E^p and G_M^p
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World data combined

- averaged and rebinned
- over BLAST range

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Impact of BLAST Results on World Data



Proton elastic form factors

- G_E^p and G_M^p
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World data combined

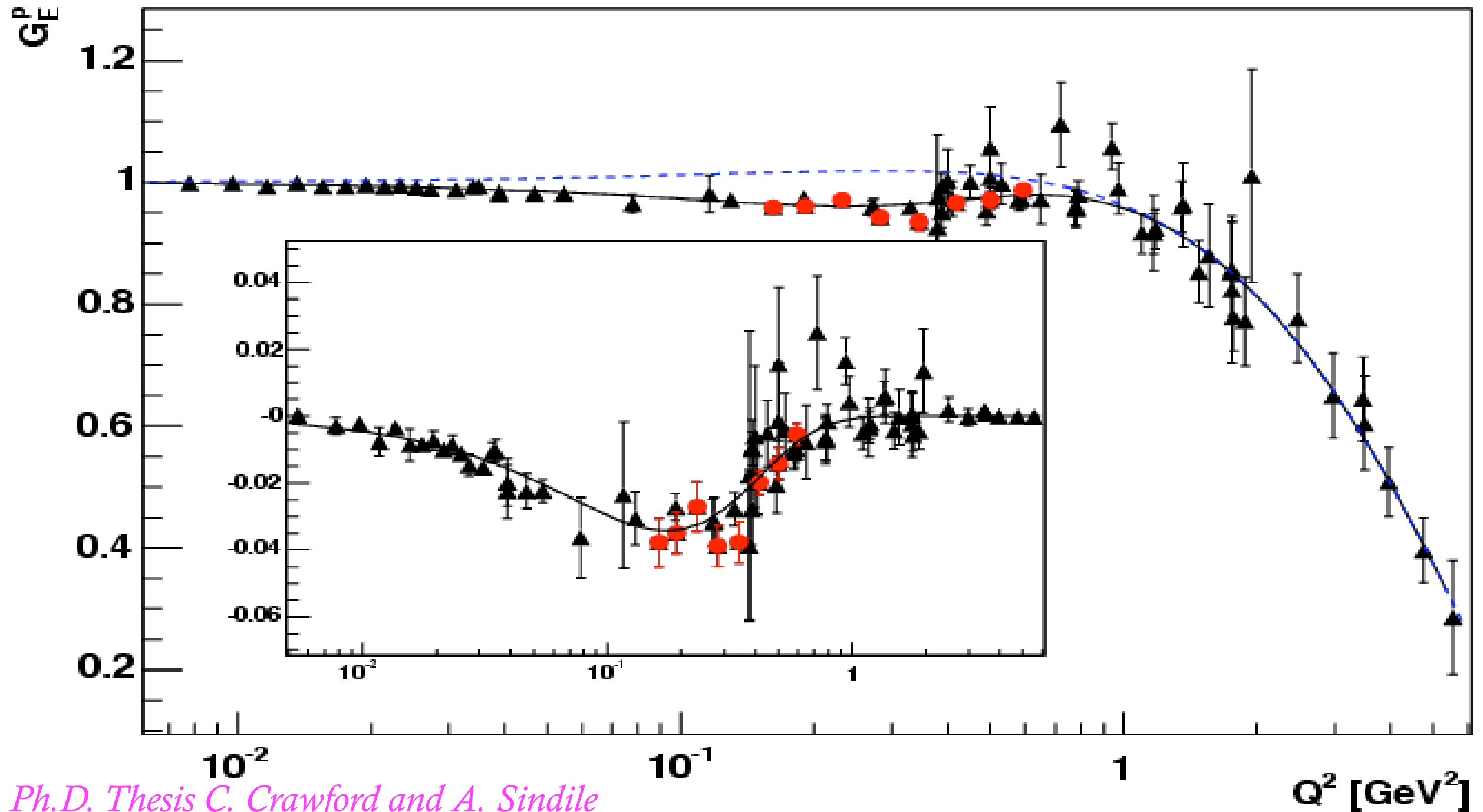
- averaged and rebinned
- over BLAST range

Constraining with BLAST

- uncertainties reduced factor 2

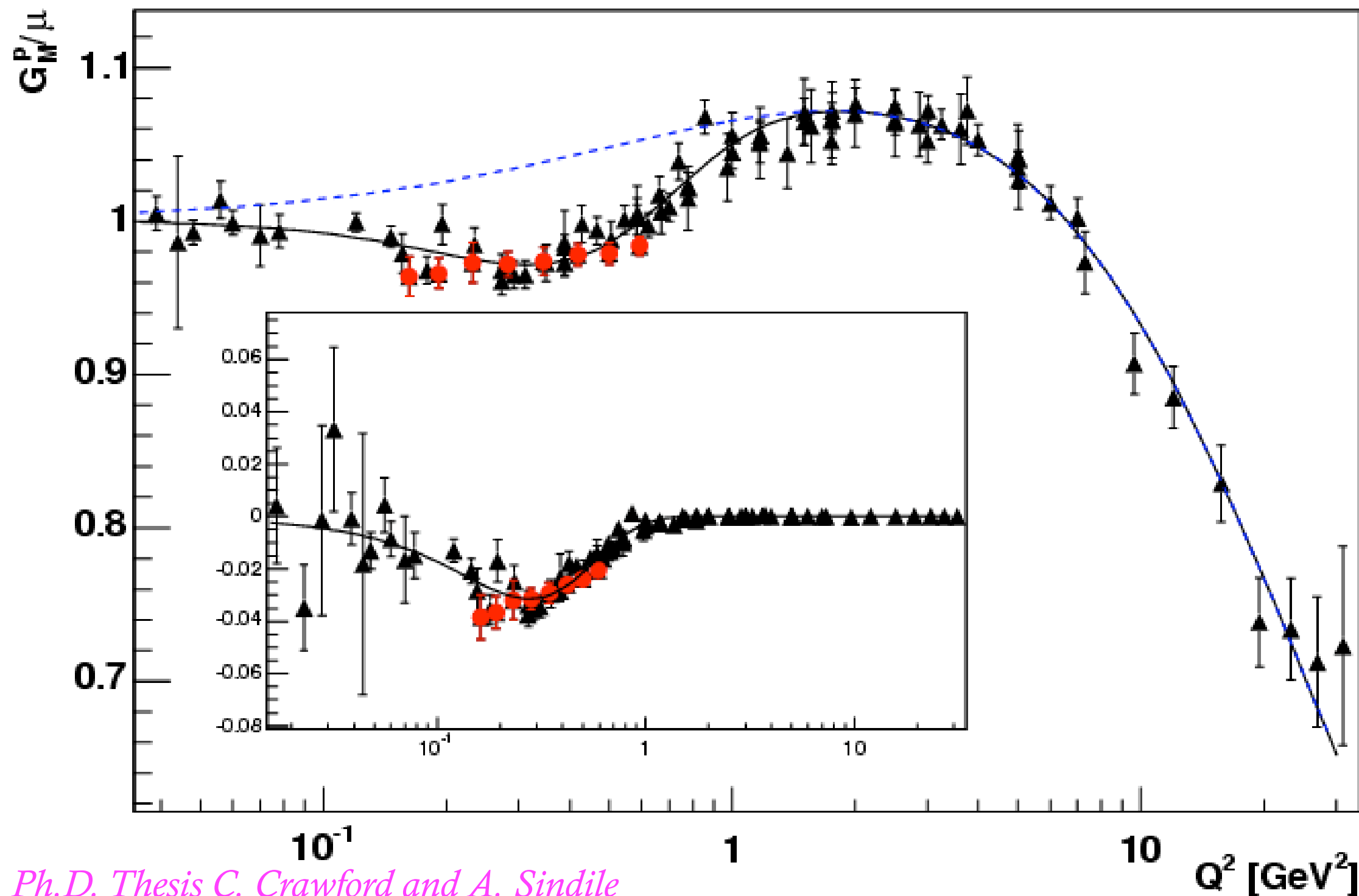
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BLAST Data with Friedrich and Walcher



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BLAST Data with Friedrich and Walcher



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Elastic Electron - Deuteron Scattering

Deuteron spin $S = 1$

- three form factors G_C^d , G_M^d , and G_Q^d
- G_Q^d arises from tensor force, D-wave
- normalisation $G_Q^d(0) = M_d^2 Q_d$

Unpolarised elastic cross section - insufficient

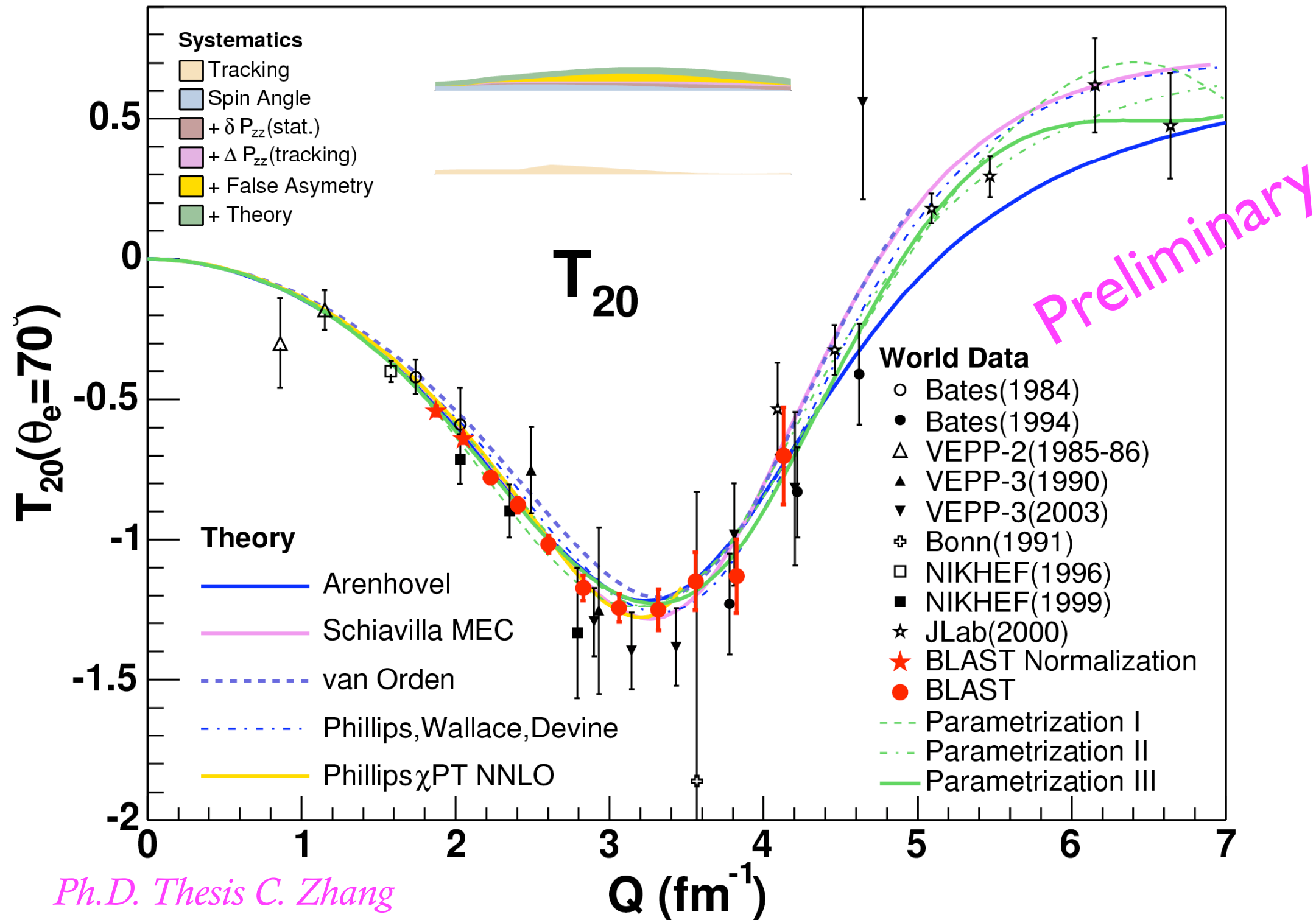
$$A(Q^2) = G_C^d{}^2 + \frac{8}{9}\eta^2 G_Q^d{}^2 + \frac{2}{3}\eta G_M^d{}^2$$

$$B(Q^2) = \frac{4}{3}\eta(1 + \eta)G_M^d{}^2; \quad \eta = Q^2 / (4M_d^2)$$

Need additional measurement - tensor asymmetry

$$T_{20} = -\frac{1}{\sqrt{2}S} \left[\frac{8}{3}\eta G_C^d G_Q^d + \frac{8}{9}\eta^2 G_Q^d{}^2 + \frac{1}{3}\eta [1 + 2(1 + \eta) \tan^2(\frac{\theta}{2})] G_M^d{}^2 \right]$$

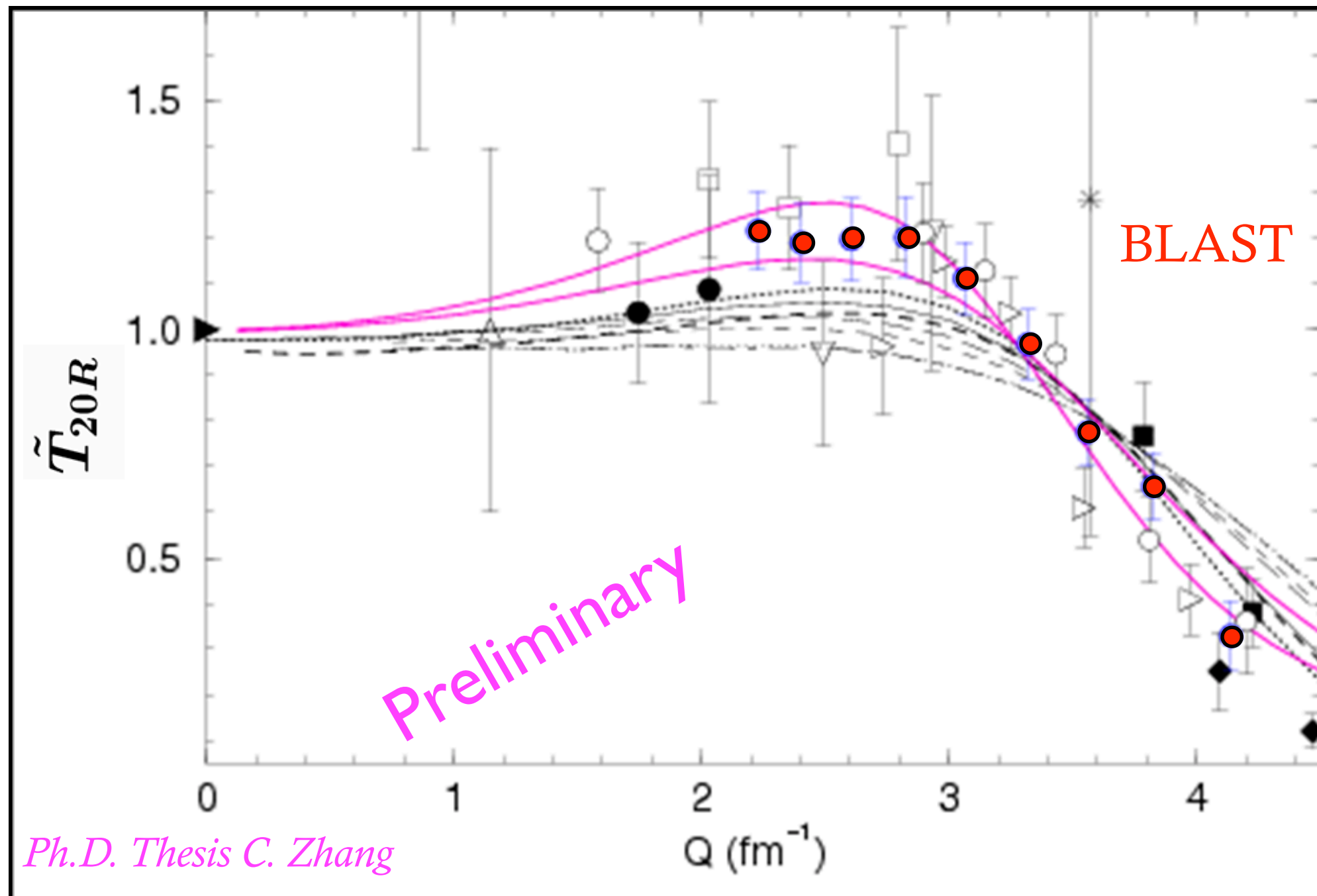
T₂₀



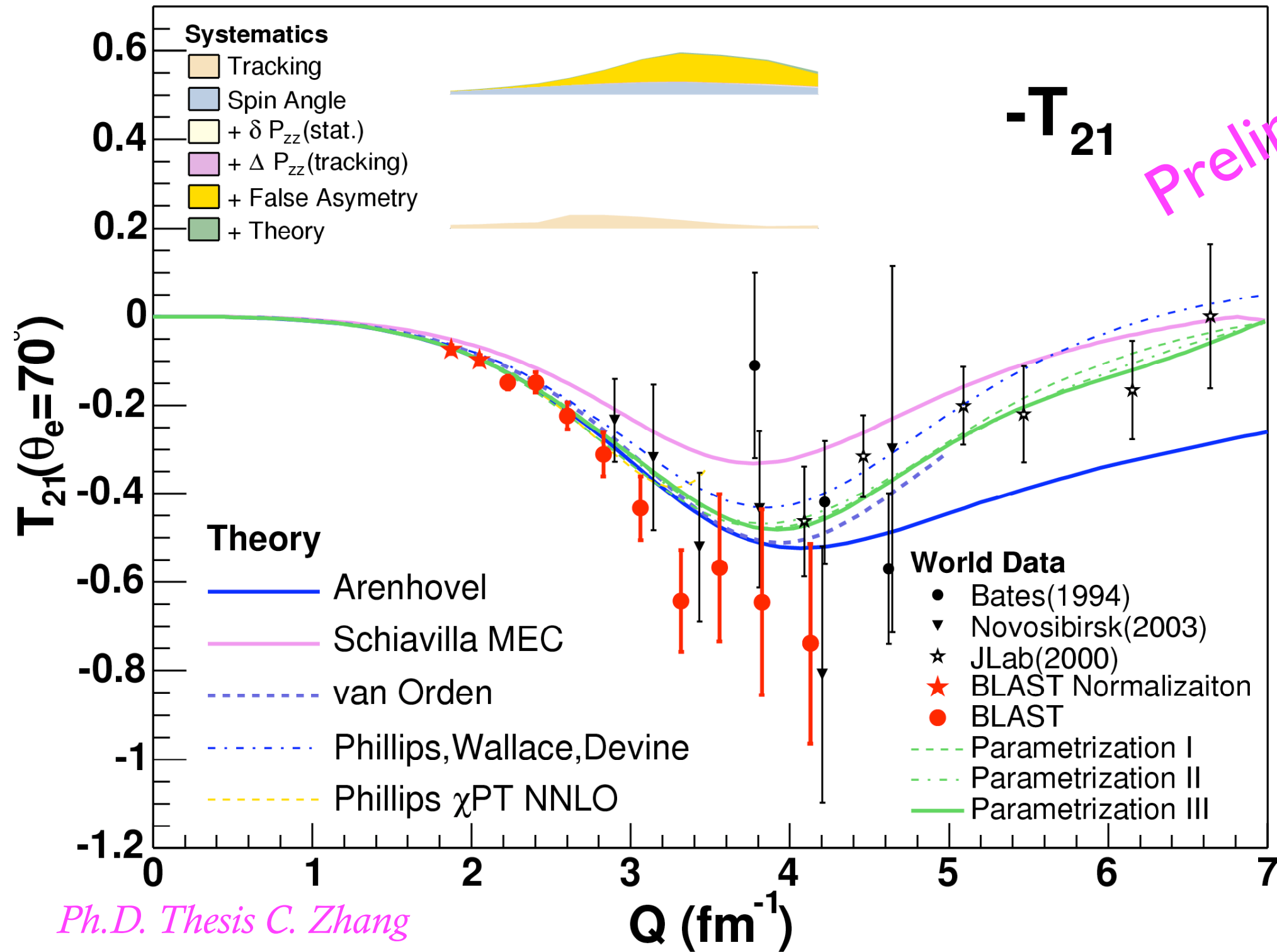
Reduced T_{20}

$$\tilde{T}_{20R} = -\frac{3}{\sqrt{2}Q_dQ^2}\tilde{T}_{20}$$

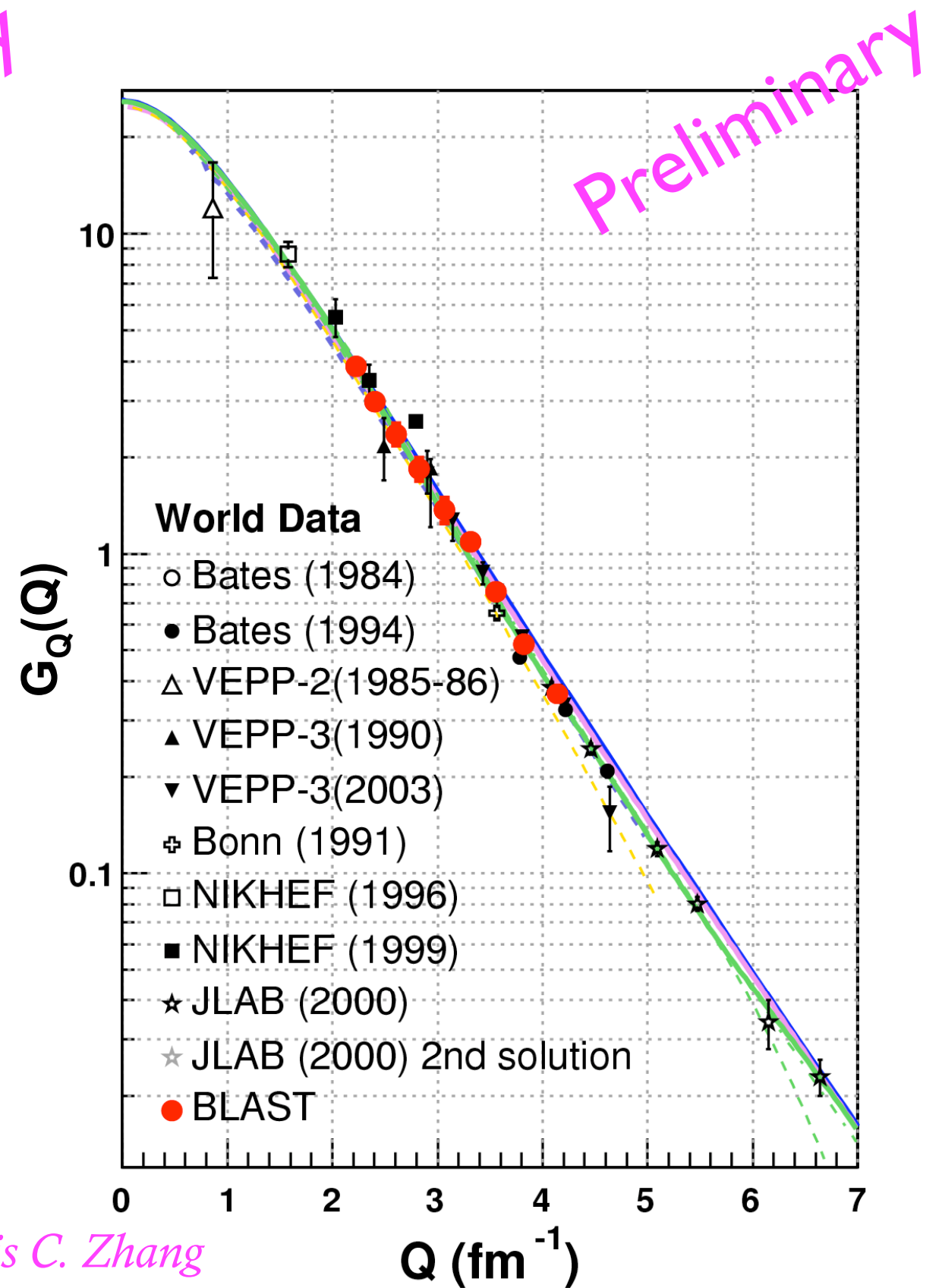
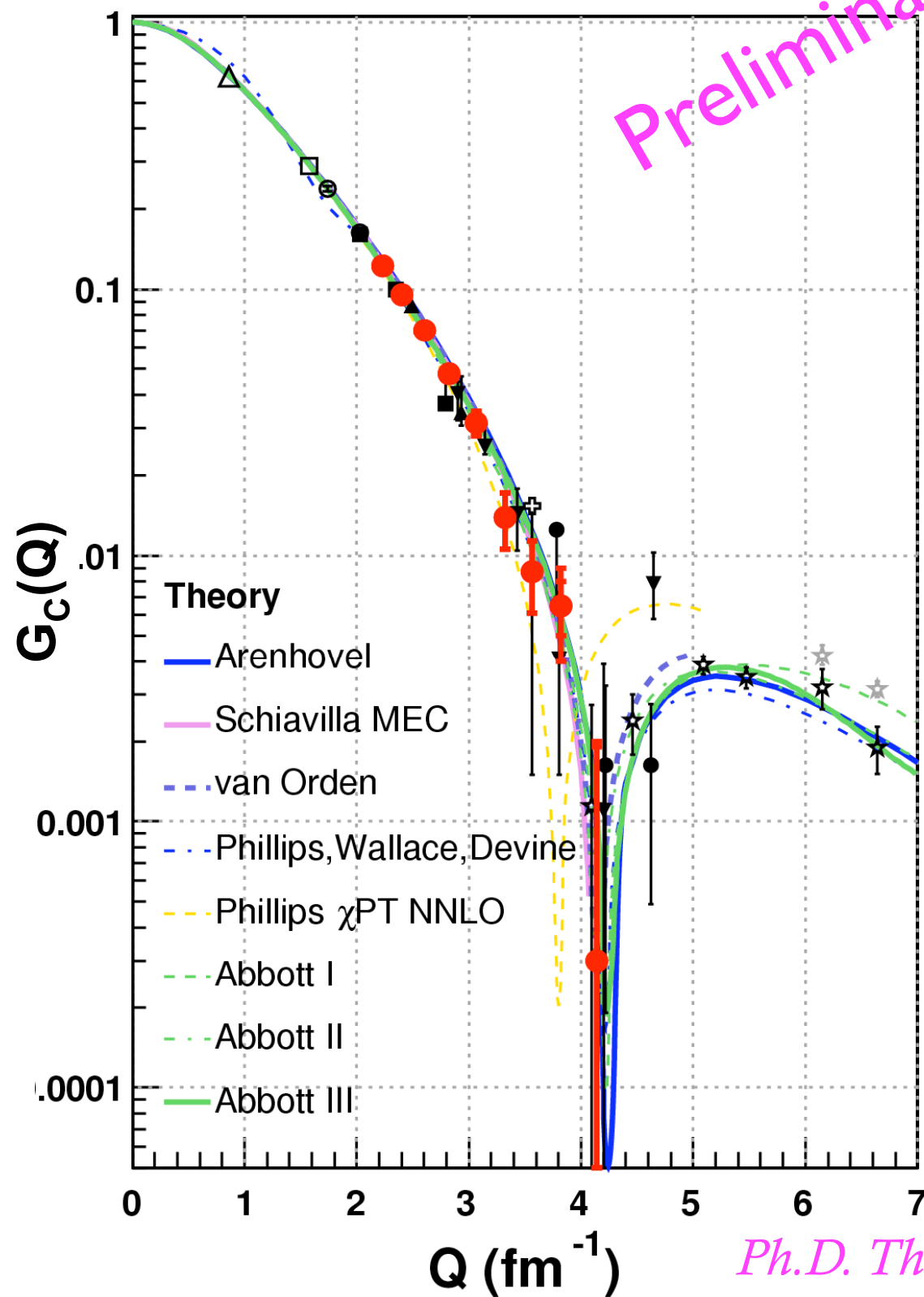
D. Phillips, J. Phys. G34, (2007) 365



T_{21}

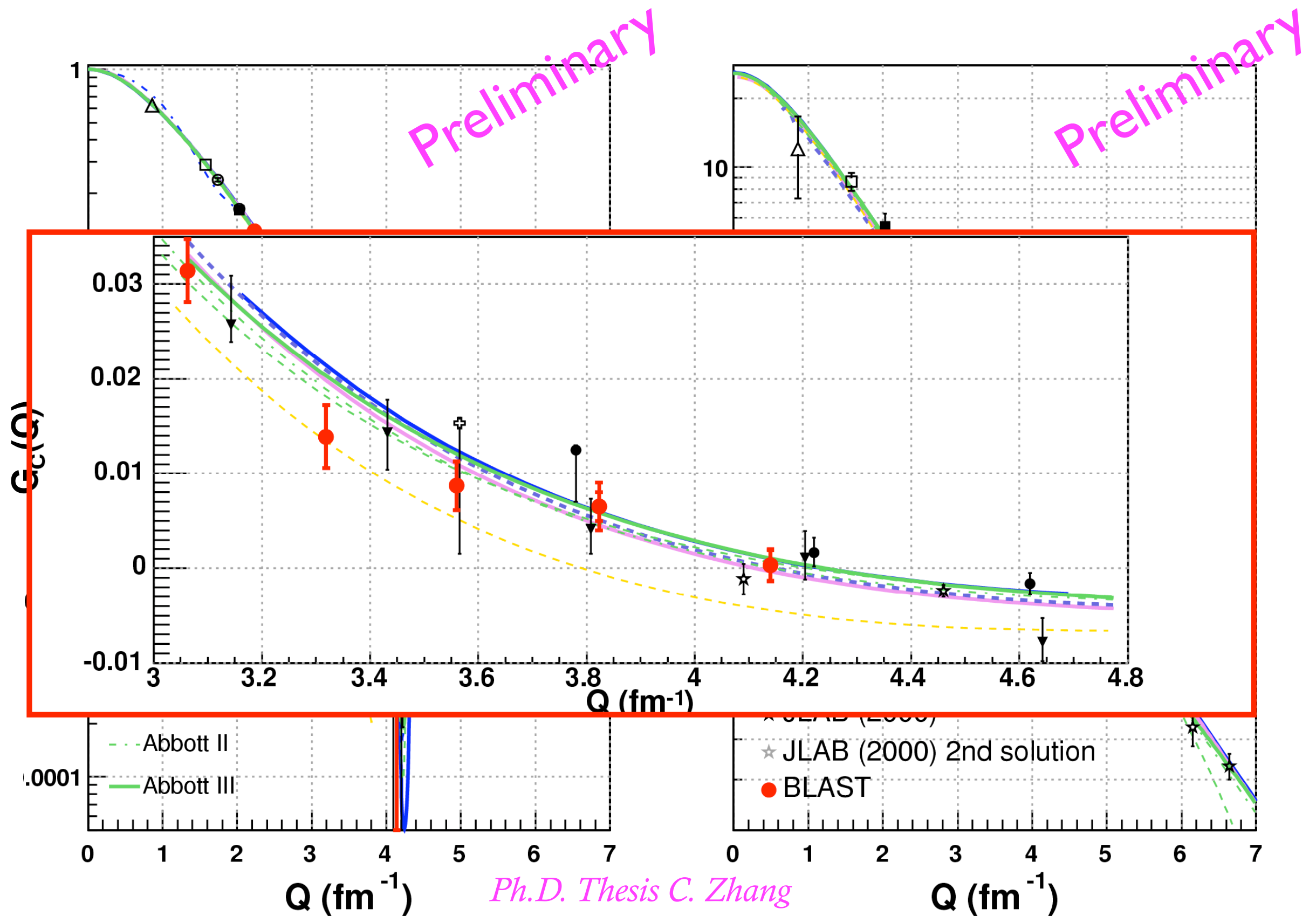


G_C and G_Q

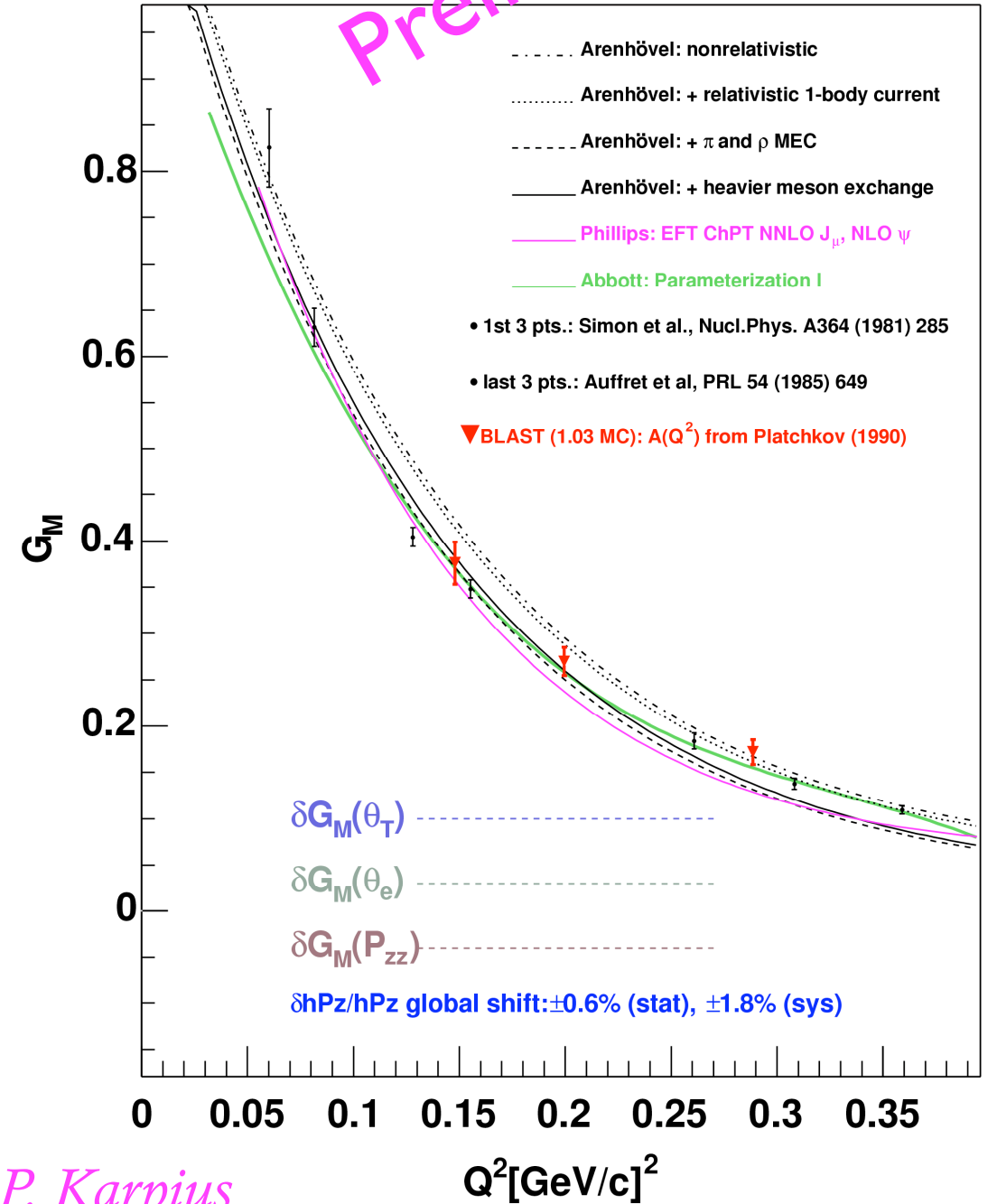
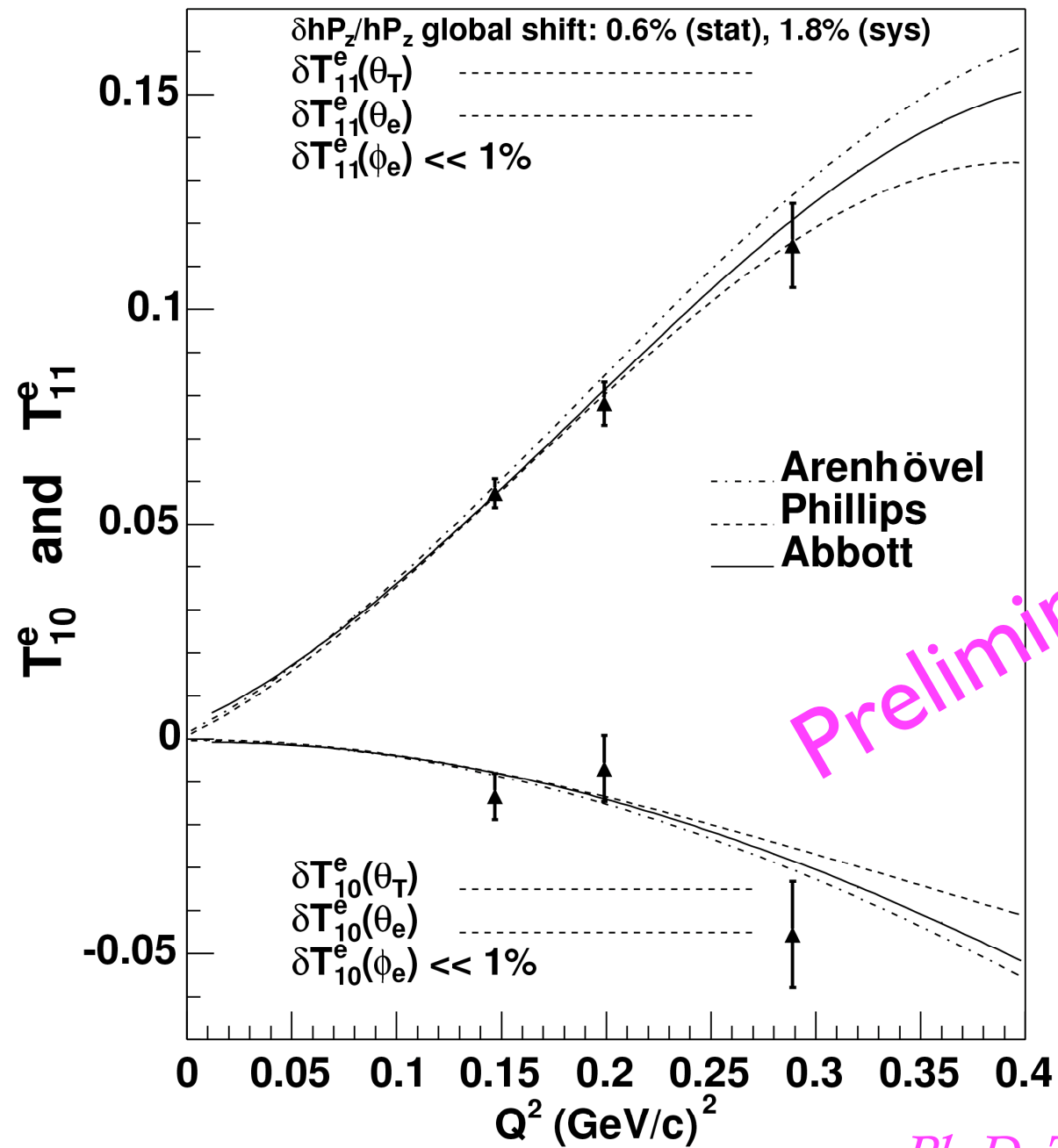


Ph.D. Thesis C. Zhang

G_C and G_Q



T_{10}^e and T_{11}^e and G_M^d



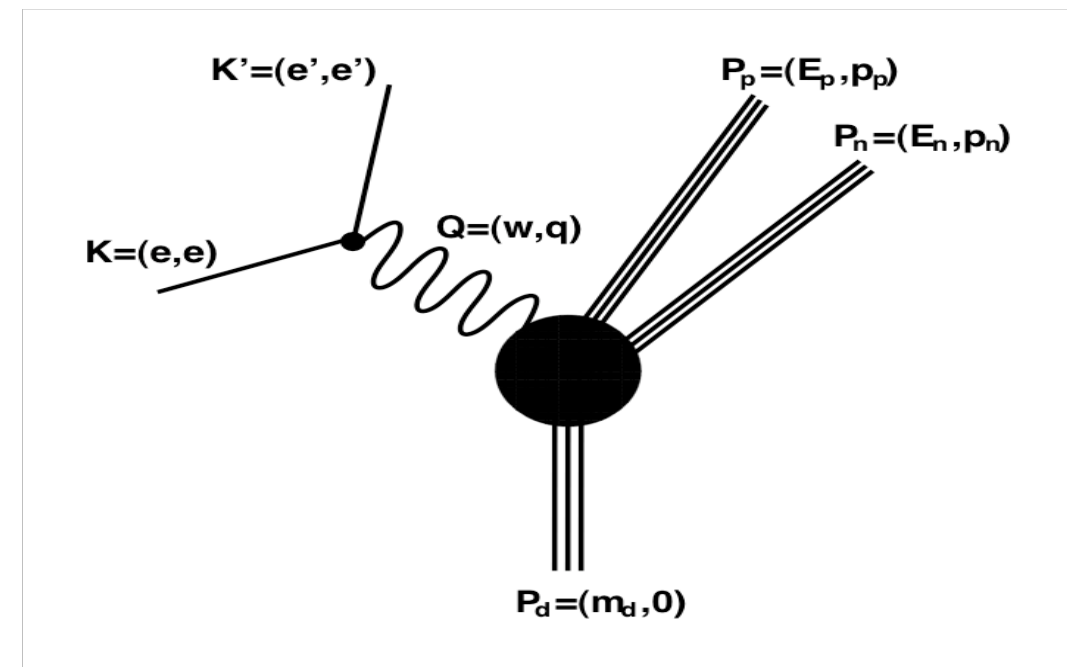
Ph.D. Thesis P. Karpus

Quasi-Elastic Scattering from Deuterium

Deuteron readily breaks up

- $e + d \rightarrow e' + p + n$
- electro-disintegration

Spin-dependent $d(e, e'N)$ cross section can be written as:



$$S(h, P_Z, P_{ZZ}) = S_0 \left[1 + P_Z A_d^V + P_{ZZ} A_d^T + h(A_e + P_Z A_{ed}^V + P_{ZZ} A_{ed}^T) \right]$$

In the Born approximation

$$A_d^V = A_e = A_{ed}^T = 0$$

Yielding:

$$S(h, P_Z, P_{ZZ}) = S_0 \left[1 + P_{ZZ} A_d^T + h P_Z A_{ed}^V \right]$$

= 0 for S state

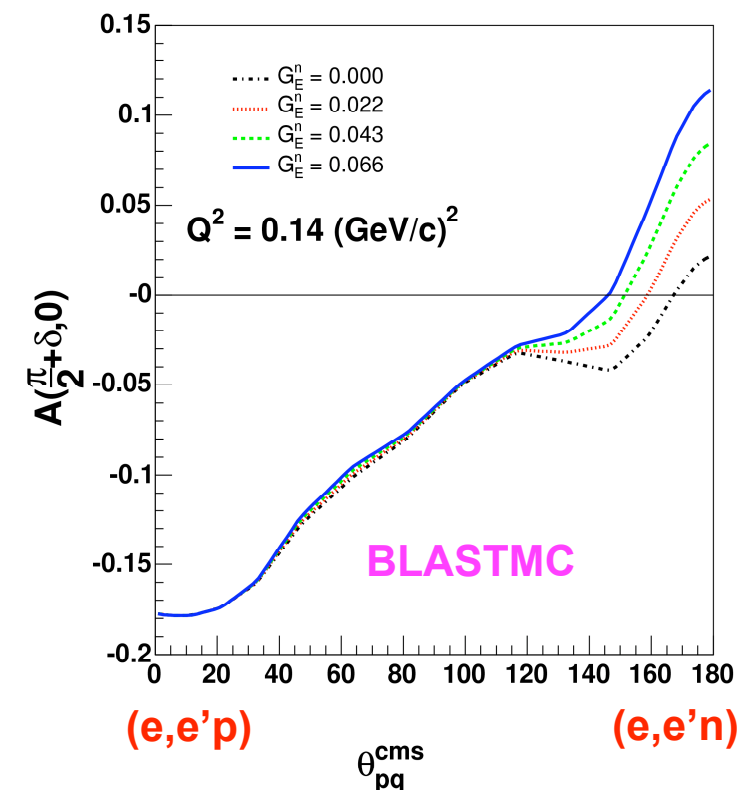
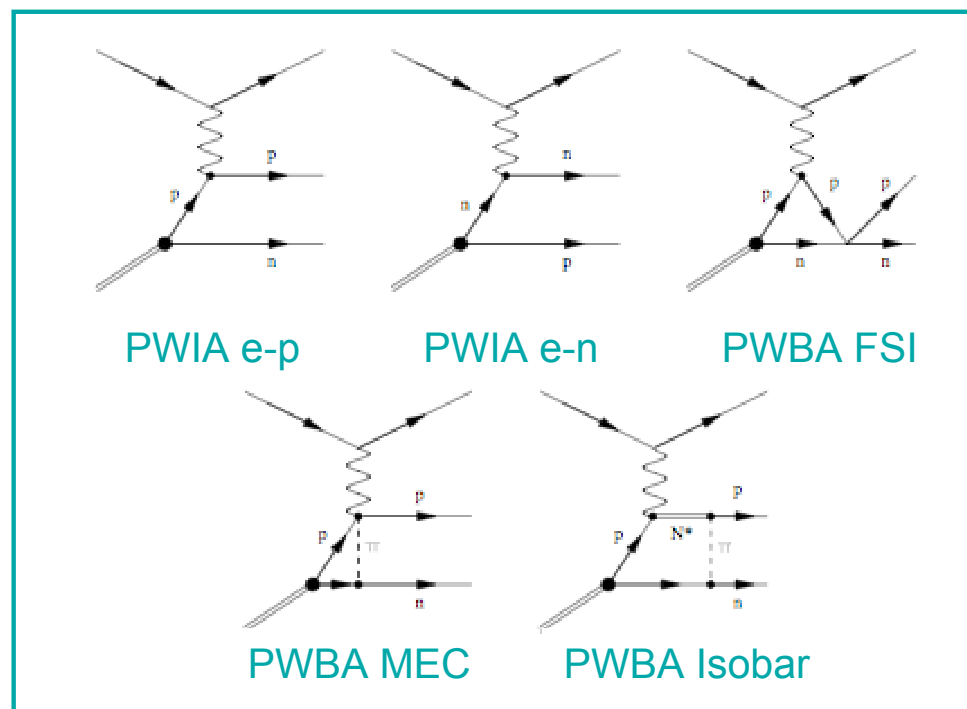
$\propto G_E/G_M$

Extracting G_E^n from A_{ed}^V

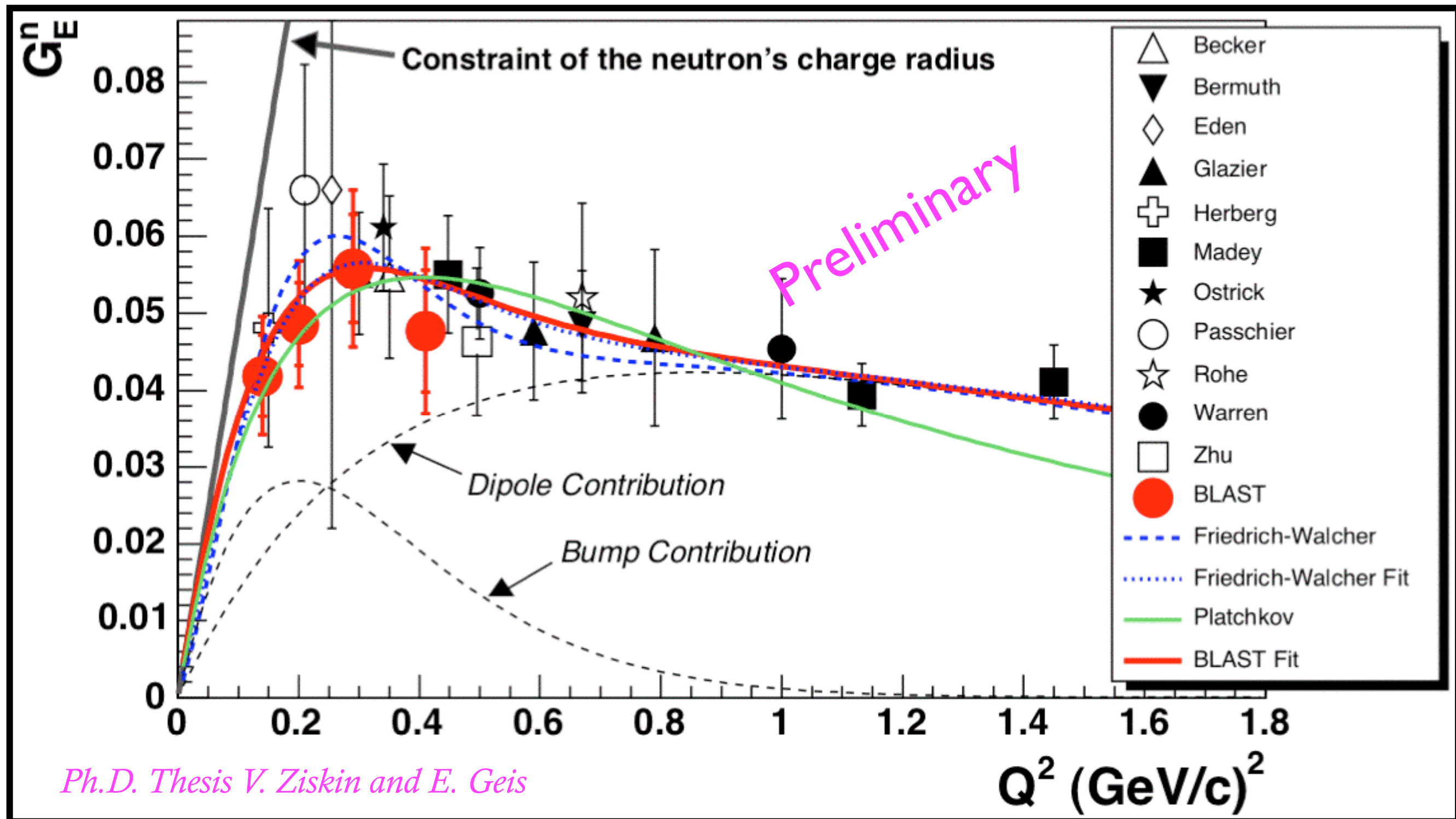
$$A_{ed}^V = \frac{a G_M^n^2 \cos \theta^* + b G_E^n G_M^n \sin \theta^* \cos \phi^*}{c G_E^n^2 + G_M^n^2} \approx a \cos \theta^* + b \frac{G_E^n}{G_M^n} \sin \theta^* \cos \phi^*$$

Beam-Target vector asymmetry gives G_E^n assuming G_M^n known

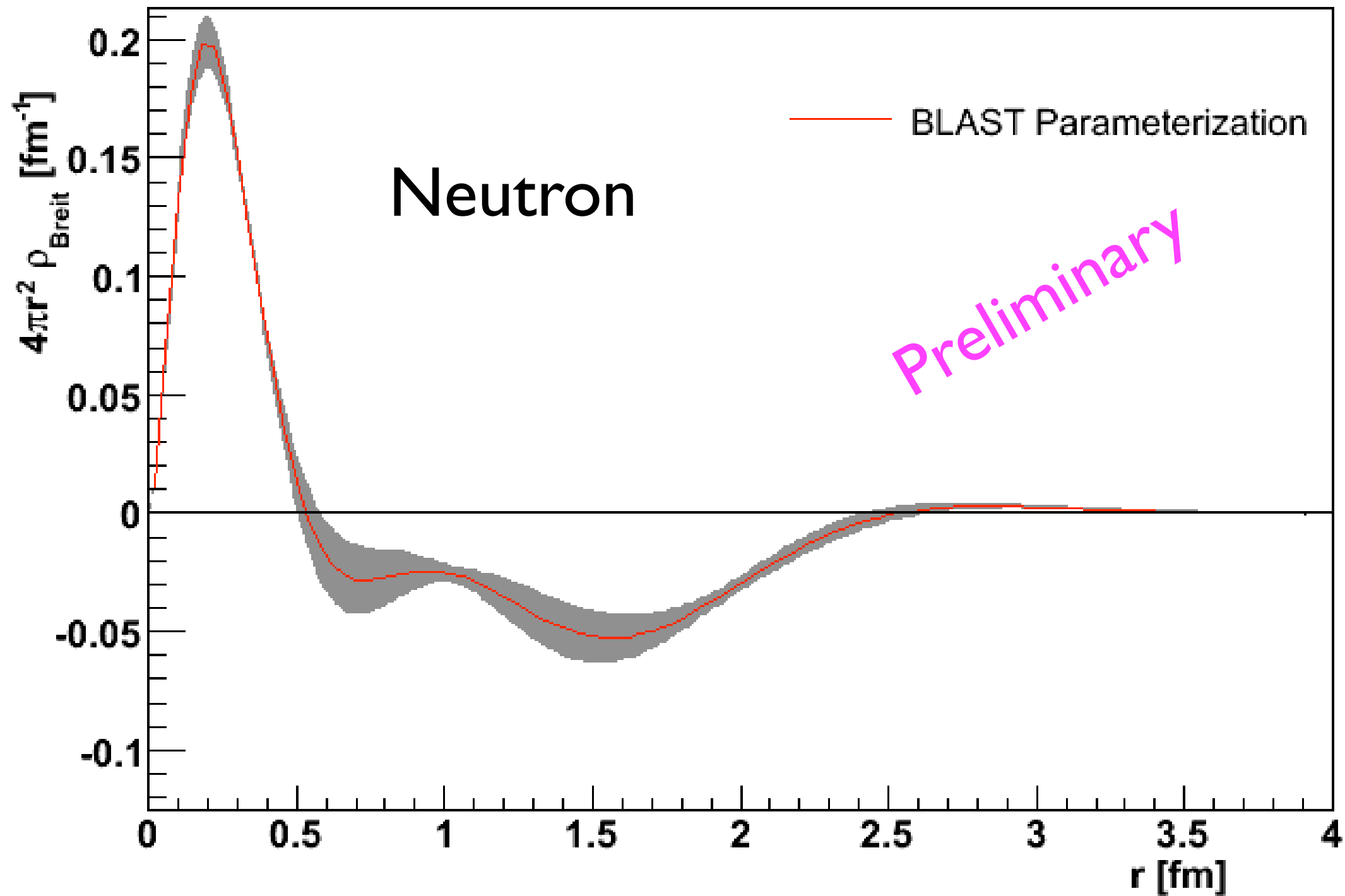
- full Monte Carlo simulation
- deuteron electro-disintegration by H. Arenhovel
- account for FSI, RC, IC, MEC
- “spin-perpendicular” kinematics shows largest effect



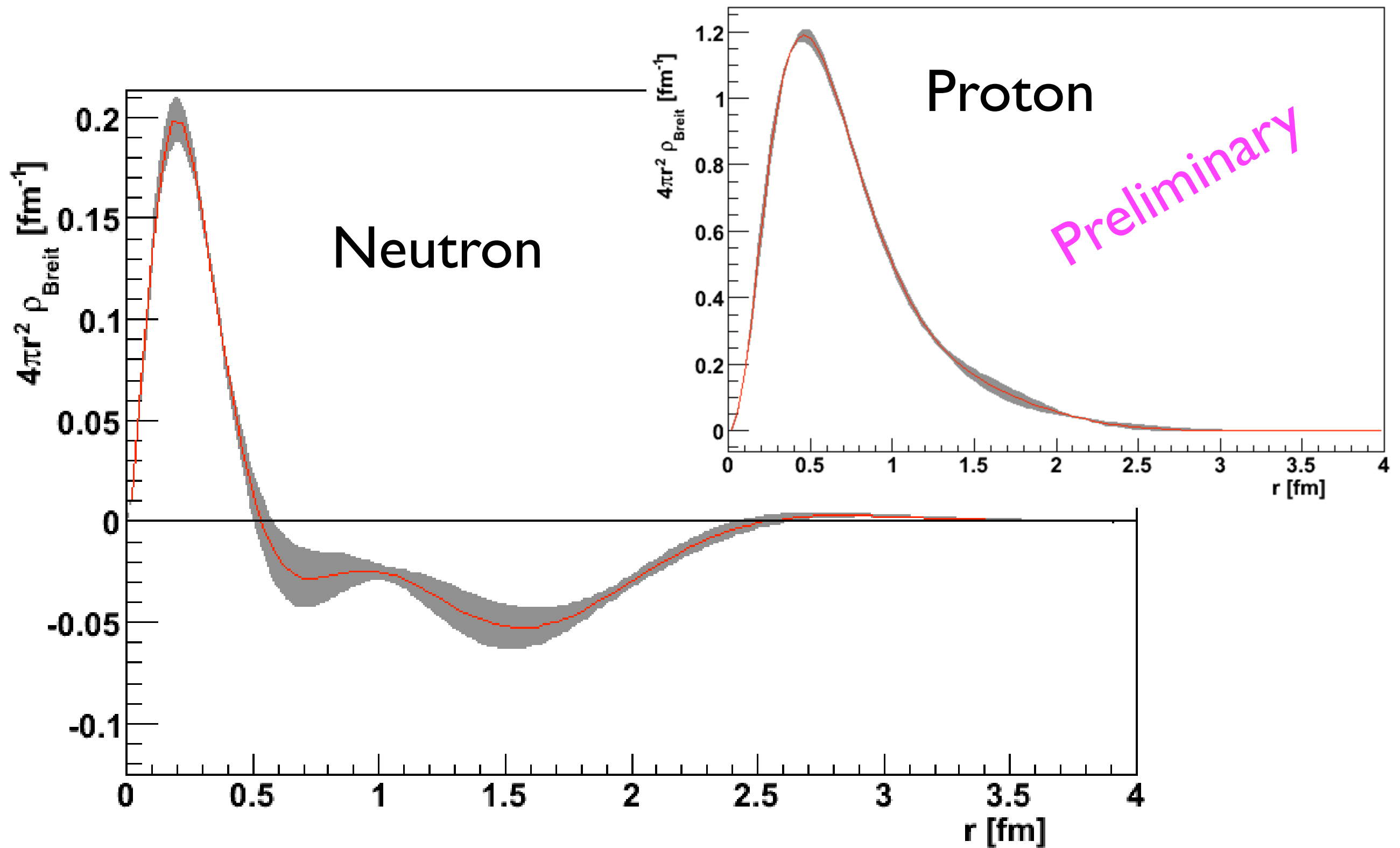
G_E^n from BLAST



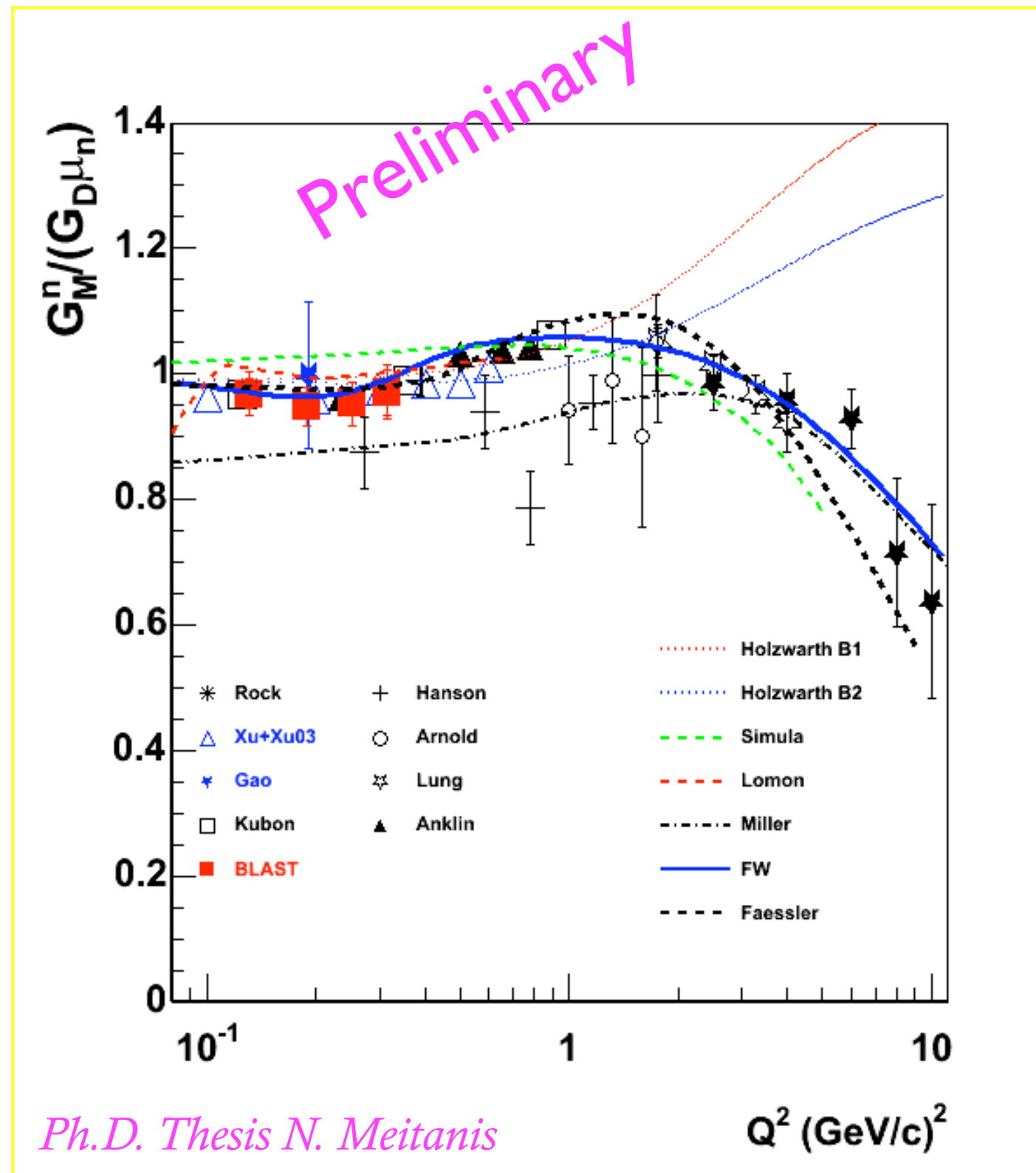
Charge Densities



Charge Densities



G_M^n from Inclusive Scattering



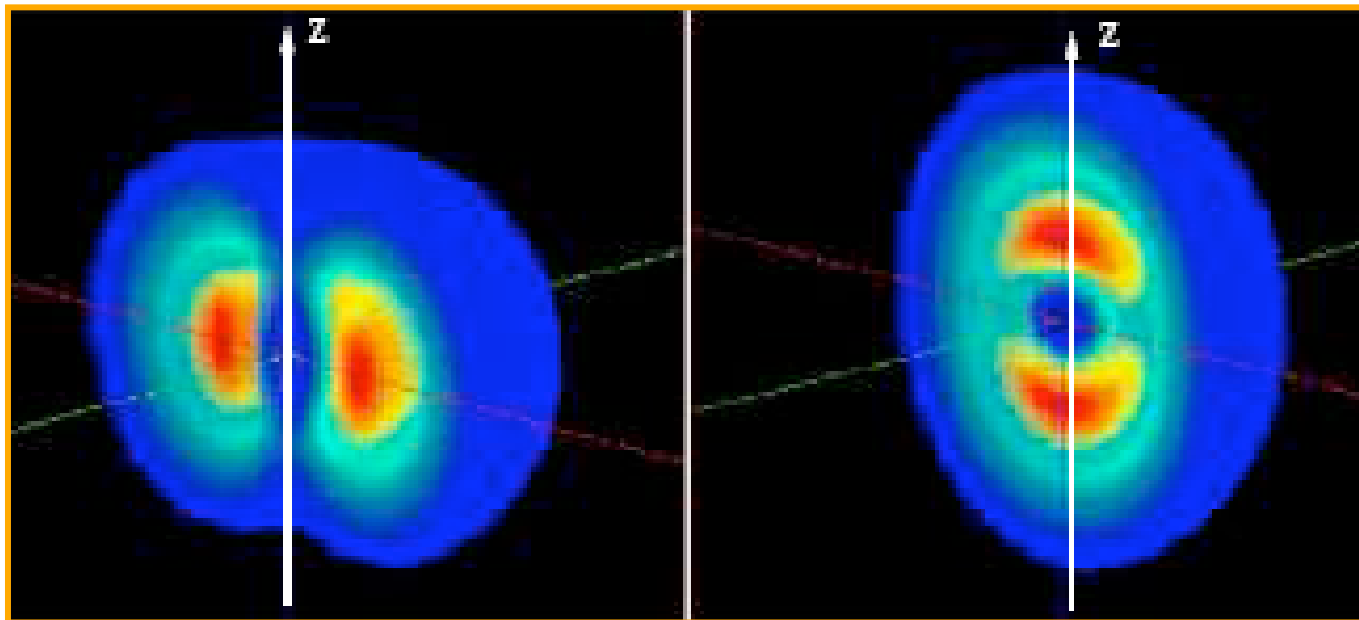
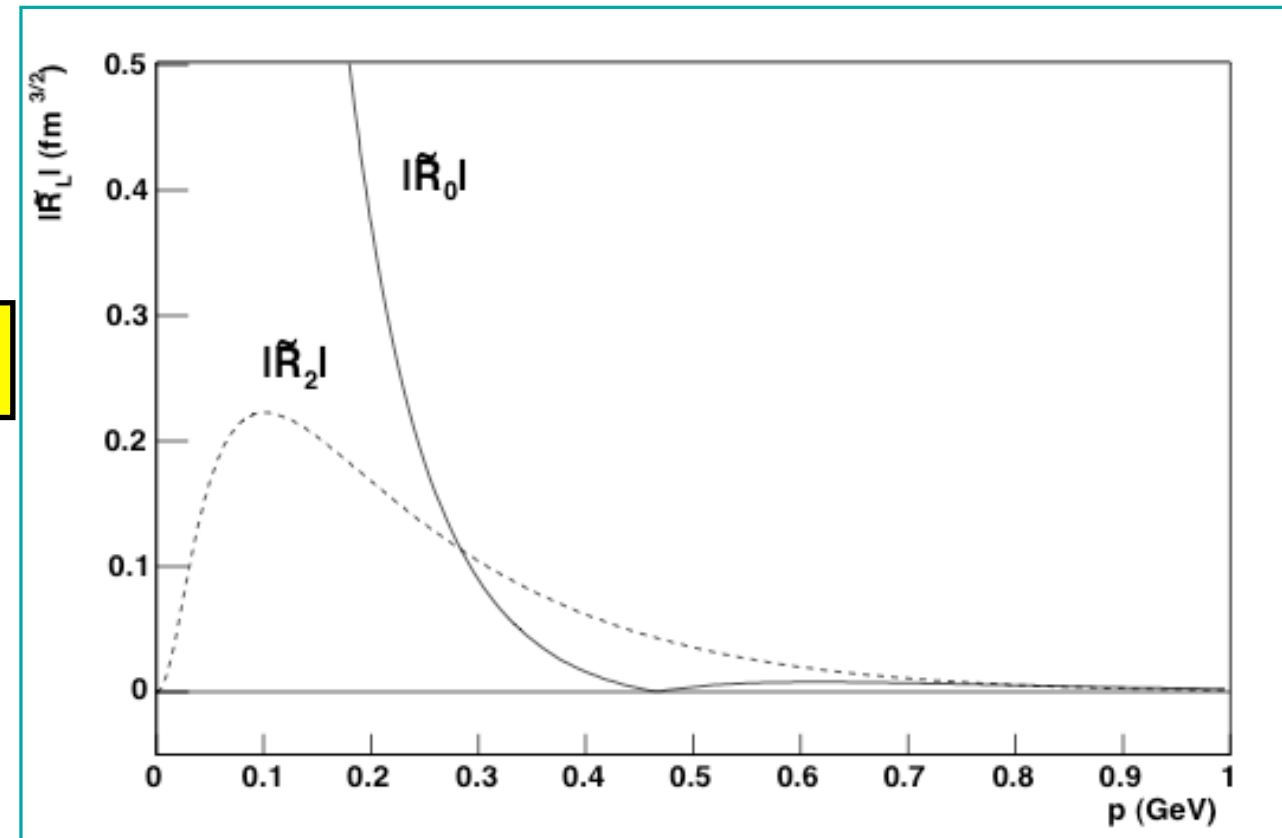
Deuteron Wavefunction

Deuteron wavefunction:

- L=0, 2 admixture

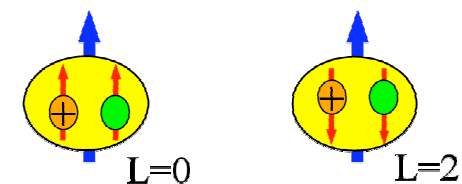
$$\psi^{m_d}(\vec{r}) = R_0(r)Y_{110}^{m_d}(\Omega_r) + R_2(r)Y_{112}^{m_d}(\Omega_r)$$

- S state minimum at $p \sim 0.45$ GeV
- D state significant at $p > 0.3$ GeV



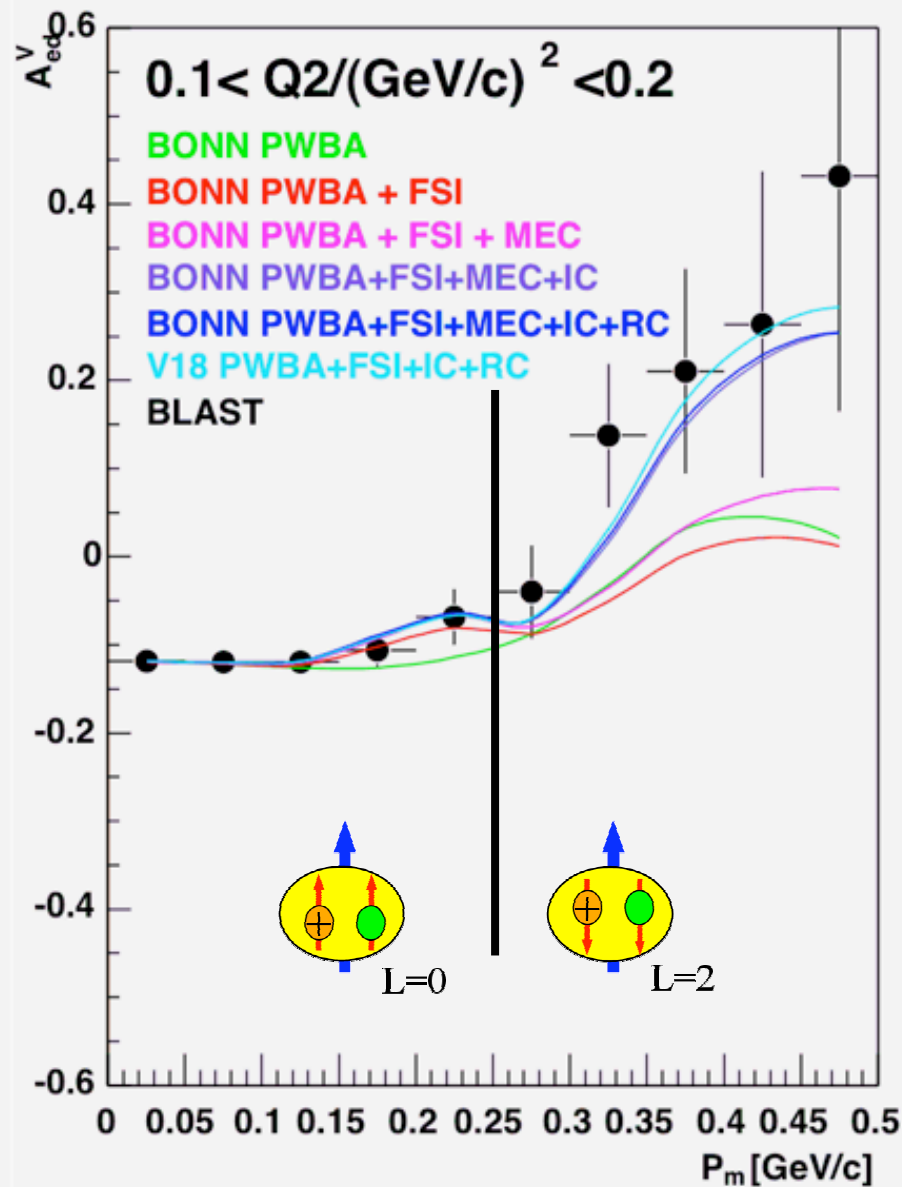
D state normally 4-6 %

- but beyond 0.3 GeV dominant
- provides a regime to study tensor force
- in D state nucleon spins flip



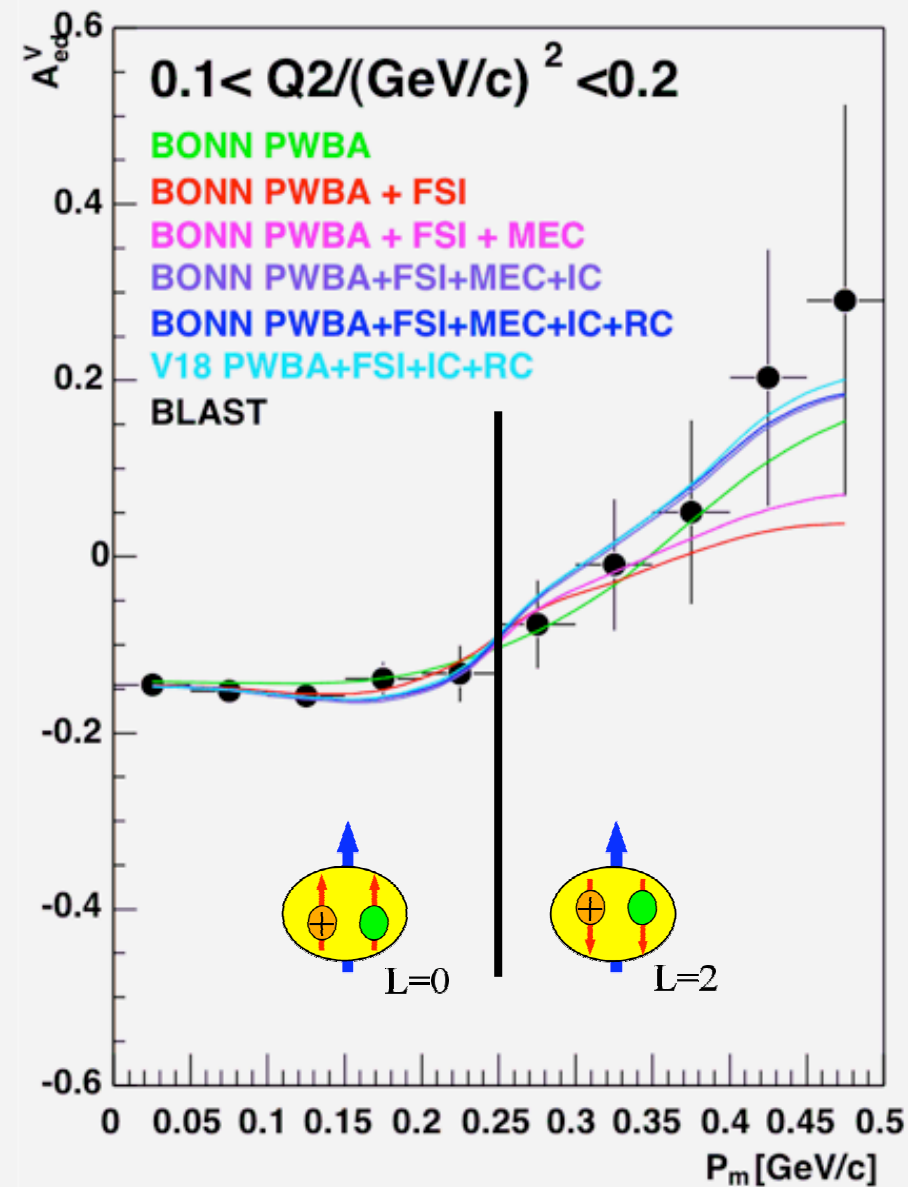
Quasi-Elastic e'p Scattering from Deuterium

47 Degrees--Perp Kine



Preliminary

47 Degrees--Para Kine



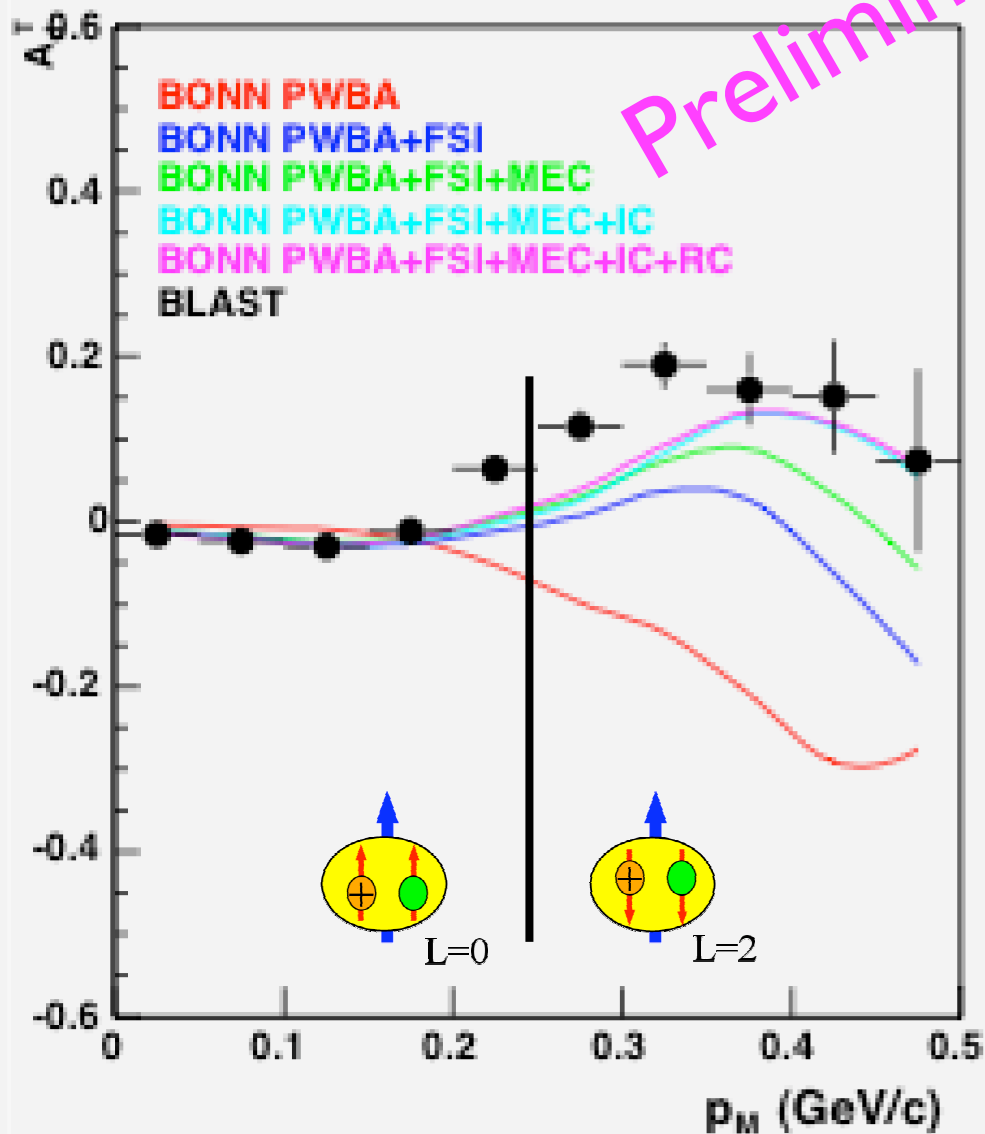
Preliminary

Ph.D. Thesis A. DeGrush

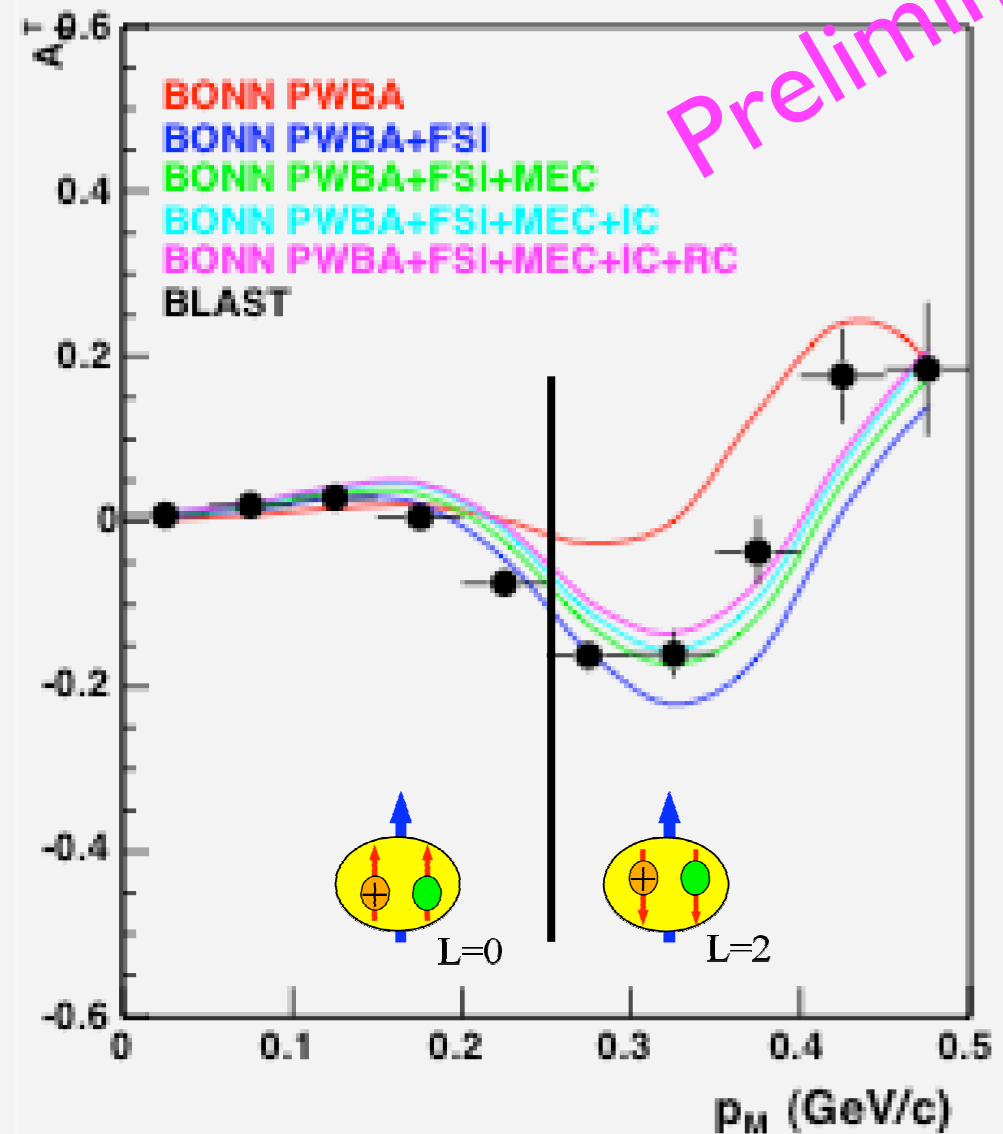
Quasi-Elastic e'p Scattering from Deuterium

$d(e,e'p)n$ Tensor Asymmetry A_d^T Vs. p_M ($0.1 \text{ GeV}^2 < Q^2 < 0.5 \text{ GeV}^2$)

Perpendicular Kinematics



Parallel Kinematics



Ph.D. Thesis A. Maschinot

BLAST Collaboration

